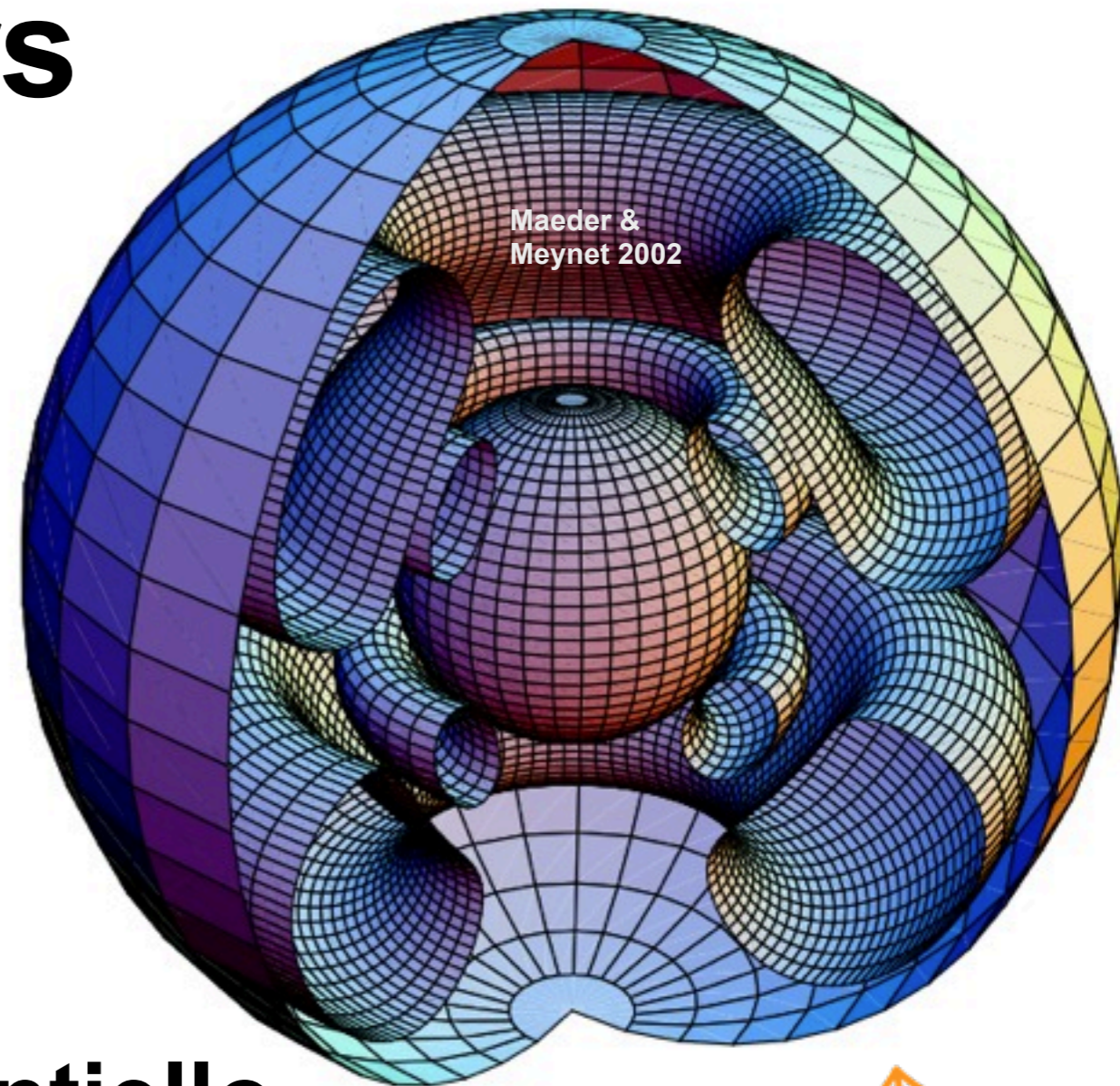
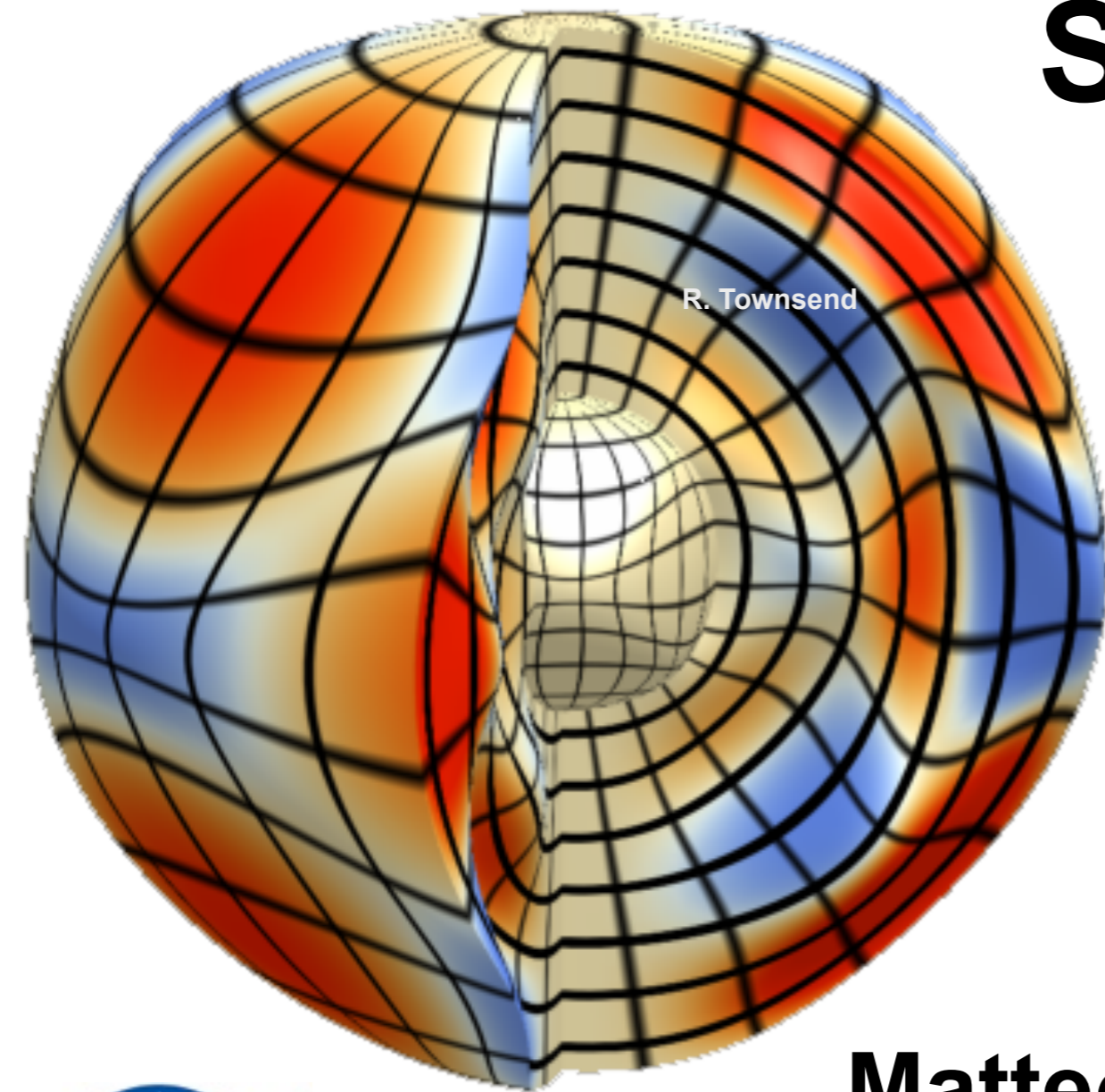


# The Physics of Stellar Angular Momentum Transport in Massive Stars



**Matteo Cantiello**

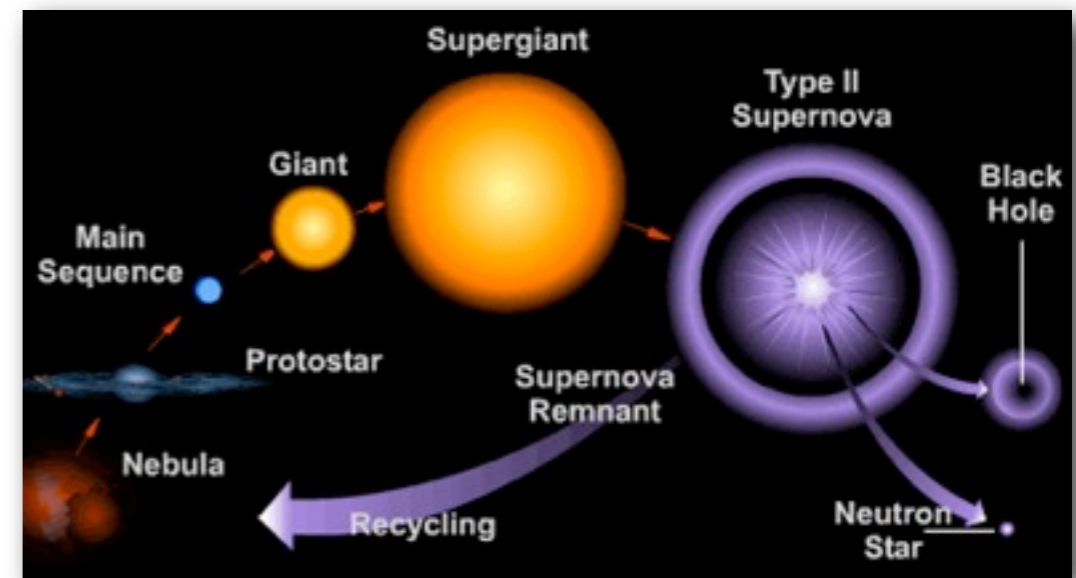
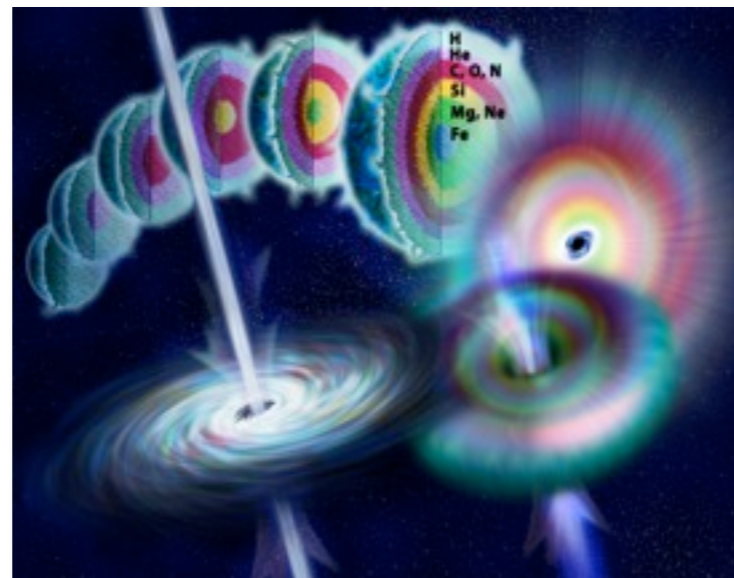
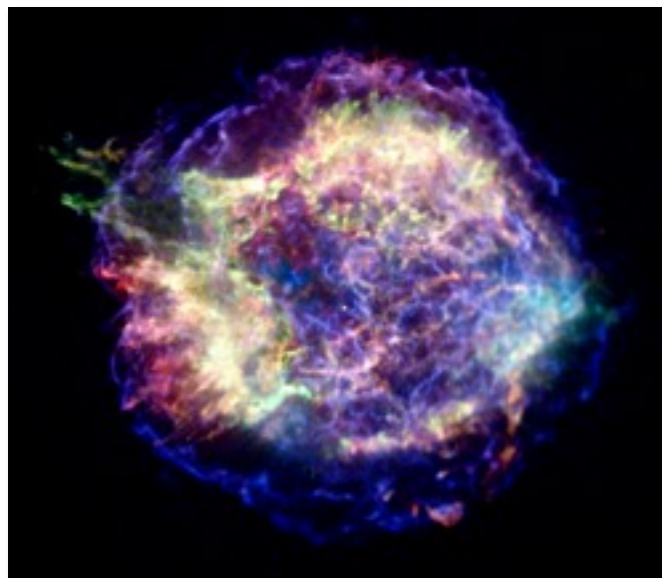
Kavli Institute for Theoretical Physics  
(University of California Santa Barbara)



**Chris Mankovich, Lars Bildsten, J.Christensen-Dalsgaard,  
Bill Paxton, Jim Fuller, Daniel Lecoanet, Ben Brown, Eliot Quataert**

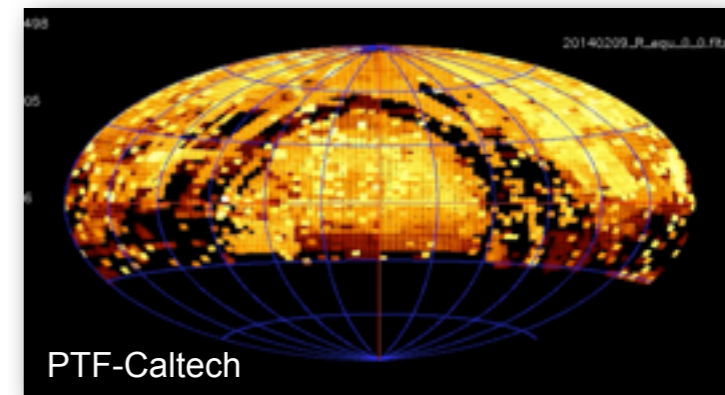
# Massive Stars

- Energy / Momentum in ISM
- Stellar Winds, SNe
- Nucleosynthesis
- Remnants: NS and BHs
- Magnetars, Pulsars, Long GRBs... Importance of magnetic fields and final angular momentum budget



# An Exciting, Rapidly Evolving Field

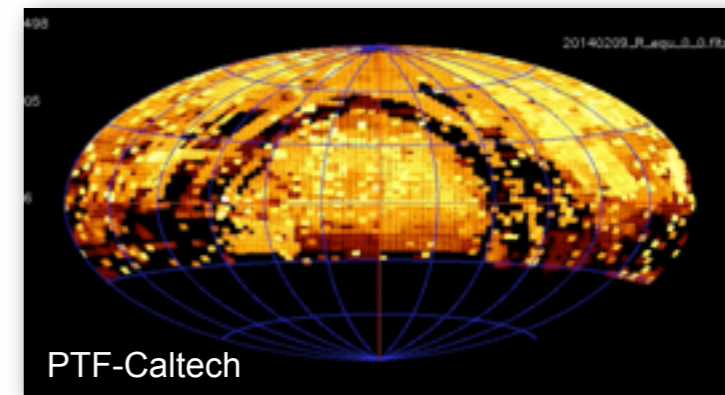
- Entering the era of high precision stellar astrophysics (CoRoT, Kepler, K2, GAIA, TESS, Plato...)
- Transient surveys revealing unexpected explosions diversity (PTF/ZTF, Pan-STARRS, LSST...)



# An Exciting, Rapidly Evolving Field

- Entering the era of high precision stellar astrophysics (CoRoT, Kepler, K2, GAIA, TESS, Plato...)
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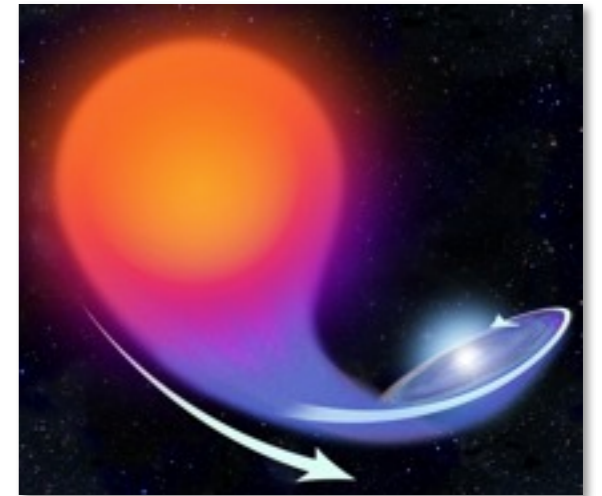
**We do NOT fully understand the evolution of Massive Stars!**



# Massive Stars in the 21st Century

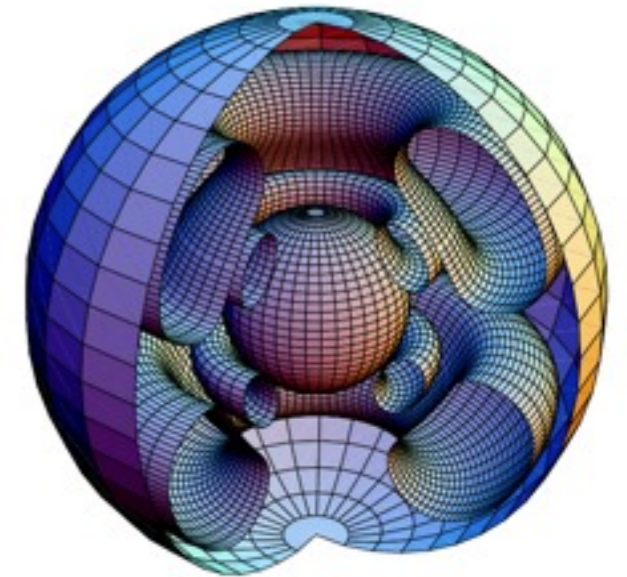
## ■ Binary Interactions

The presence of a close companion can significantly influence the evolution of massive stars (e.g. [Podsiadlowski+ 1992](#), [Cantiello+ 2007](#), [Langer+ 2008](#), [Eldridge+ 2011](#))



## ■ Rotation

Stellar rotation has also a profound impact on the evolution of massive stars. In particular the final fate of rapidly rotating stars is expected to differ significantly from slowly rotating ones. (e.g. [Yoon+ 2006](#), [Woosley+ 2006](#))



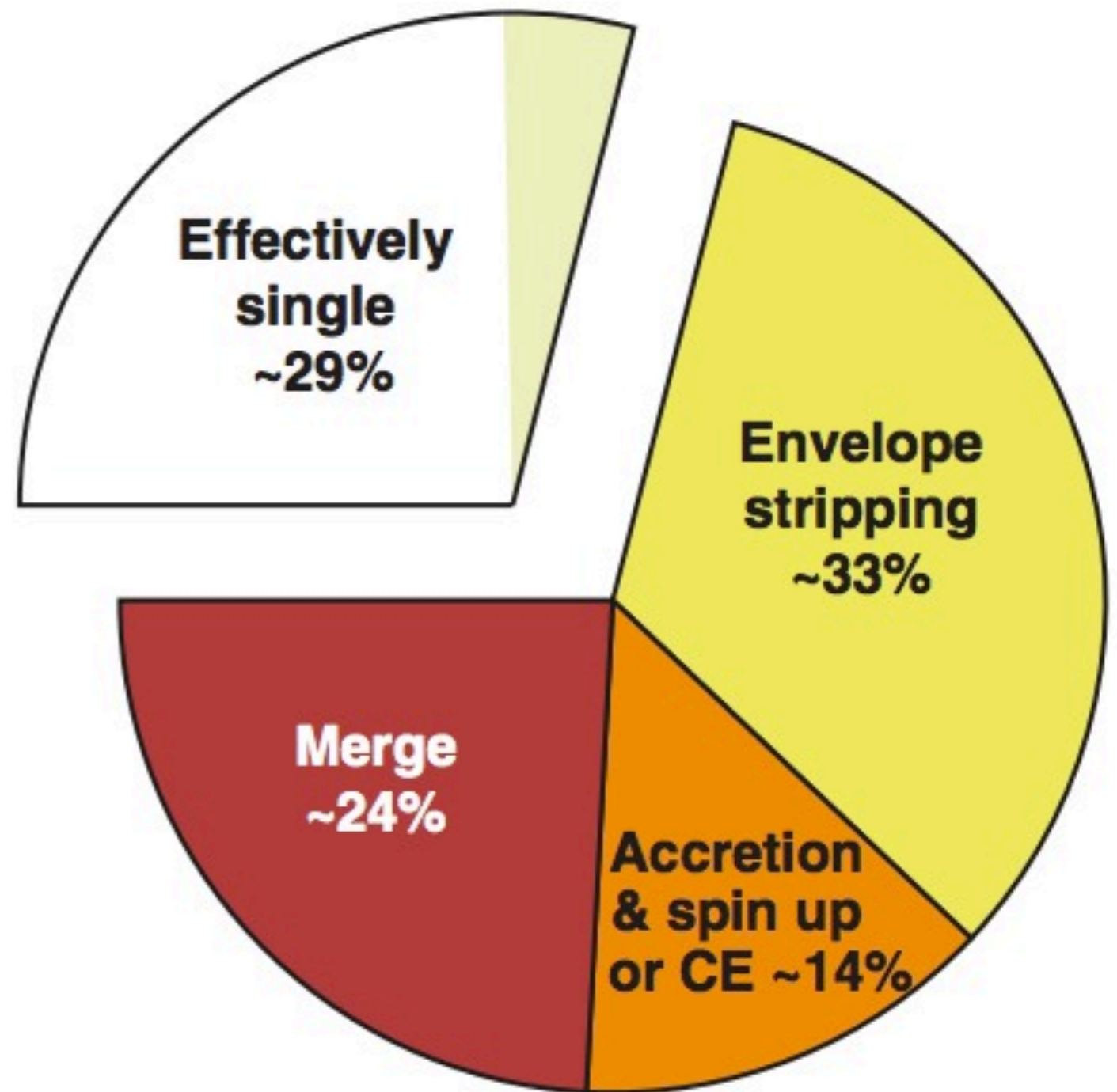
## ■ Magnetic Fields

Magnetic fields can potentially affect the evolution of massive stars and their explosive deaths. At this stage little is known about the prevalence and amplitude of (internal) magnetic fields (e.g. [Spruit 2002](#), [Heger+ 2005](#), [Cantiello & Braithwaite 2010](#), [MiMES](#))



# Binary Interactions are the norm

**“71% of all stars born as O-type interact with a companion, over half of which do so before leaving the main sequence”**



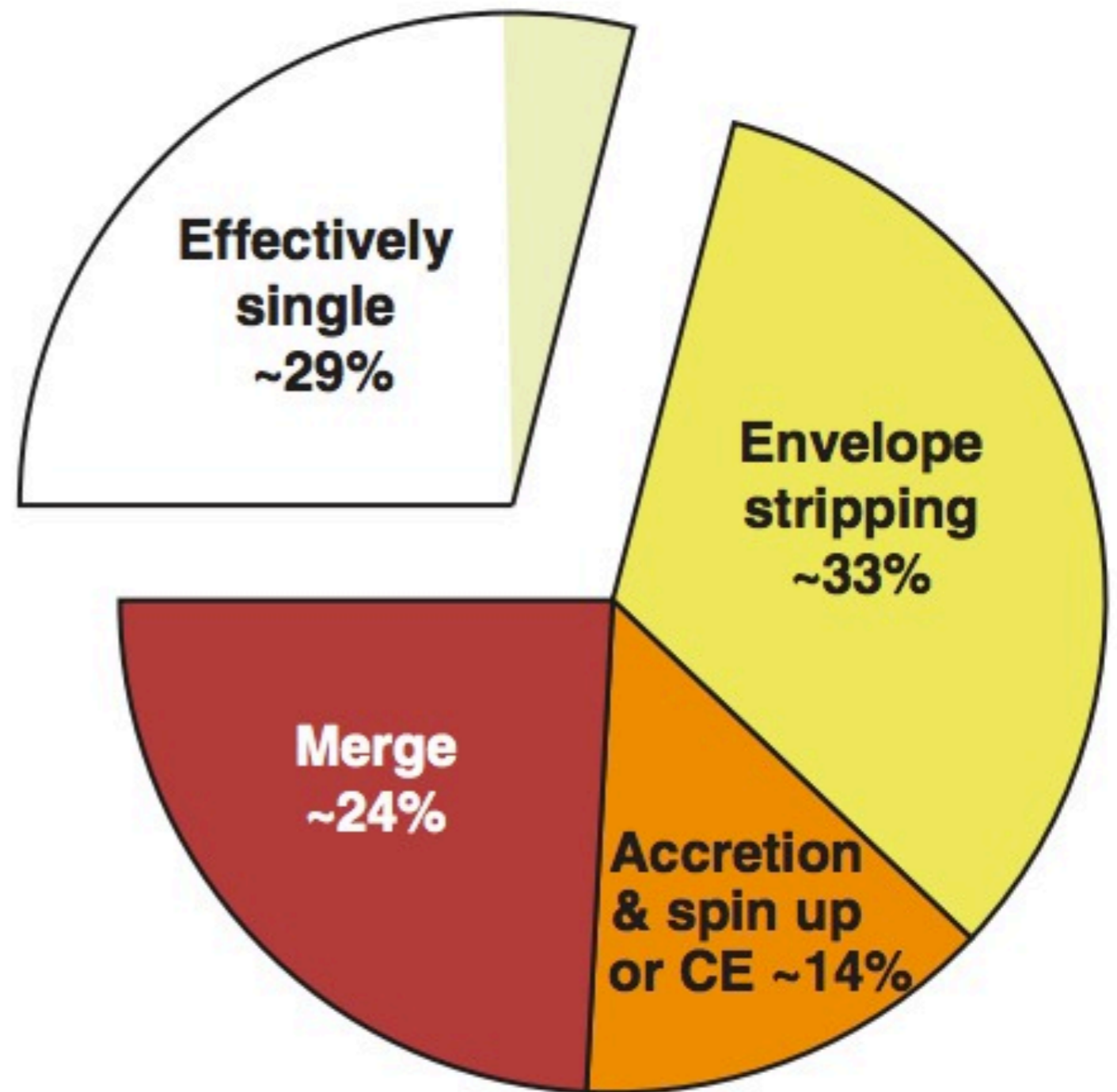
Sana et al. 2012 (Science)

# Binary Interactions are the norm

**Numbers for  
B-type stars  
look similar**

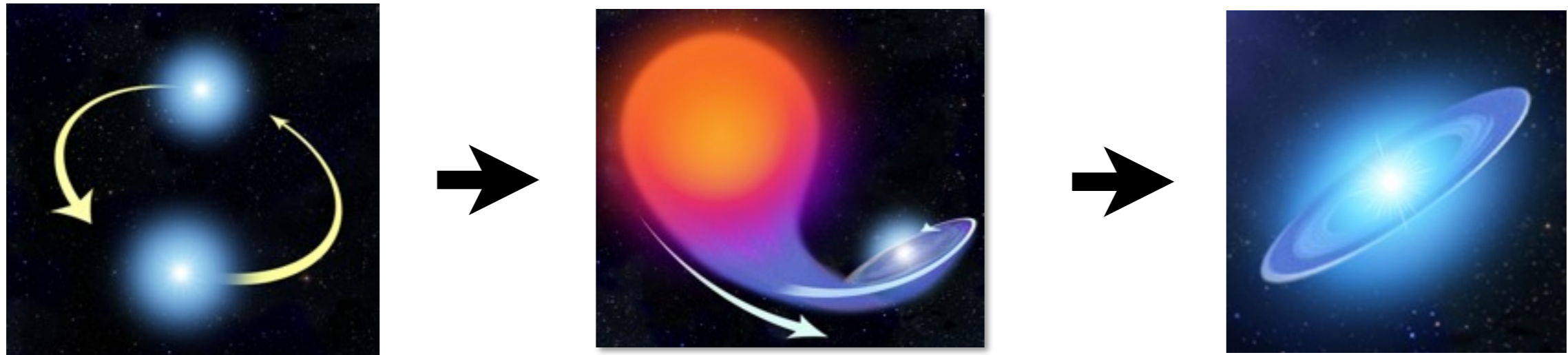
Dunstall et al. 2015

**A large fraction of  
CCSN progenitors  
interacted with a  
binary companion**



Sana et al. 2012 (Science)

# Binary Interactions are the norm



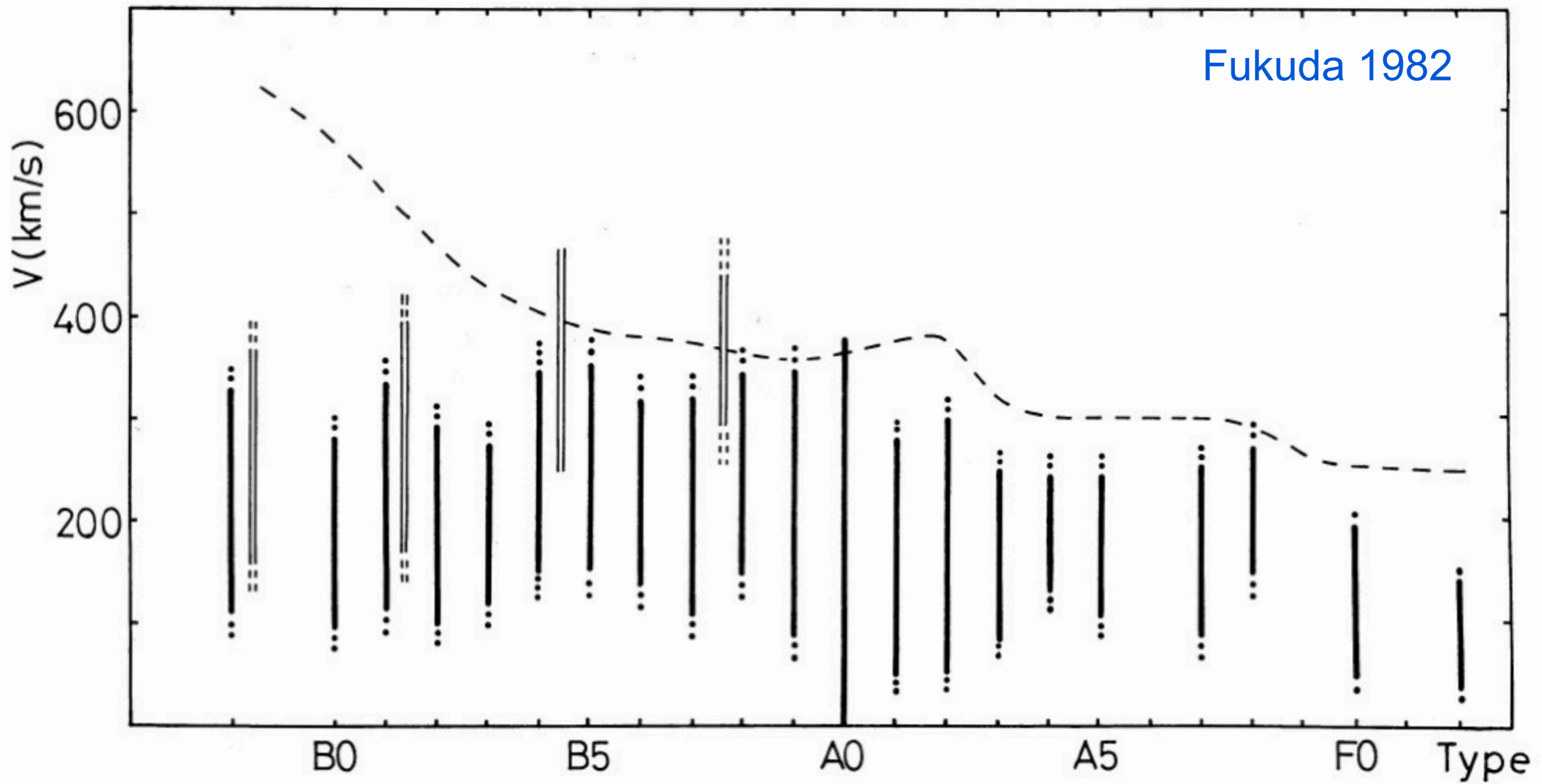
- Tides, mass transfer and stellar mergers are expected to largely change the rotational properties of stars
- To fully understand binary interactions (and SN progenitors) we **first need to understand the physics of stellar rotation** (in single stars)



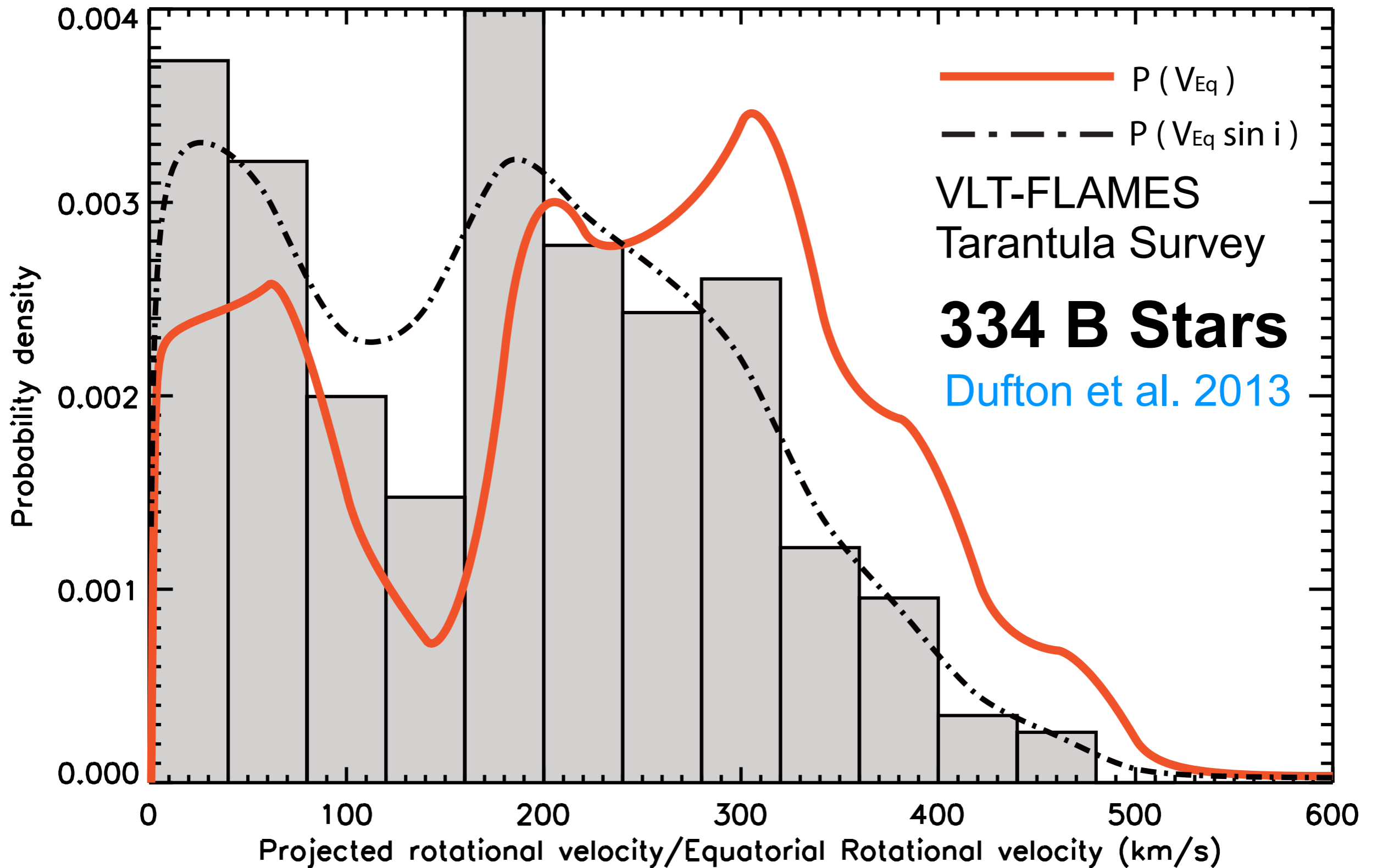
**Stars are born rotating**

# Range of rotational velocity

“In practice **all stars** are rotating around their axis” - Maeder & Meynet



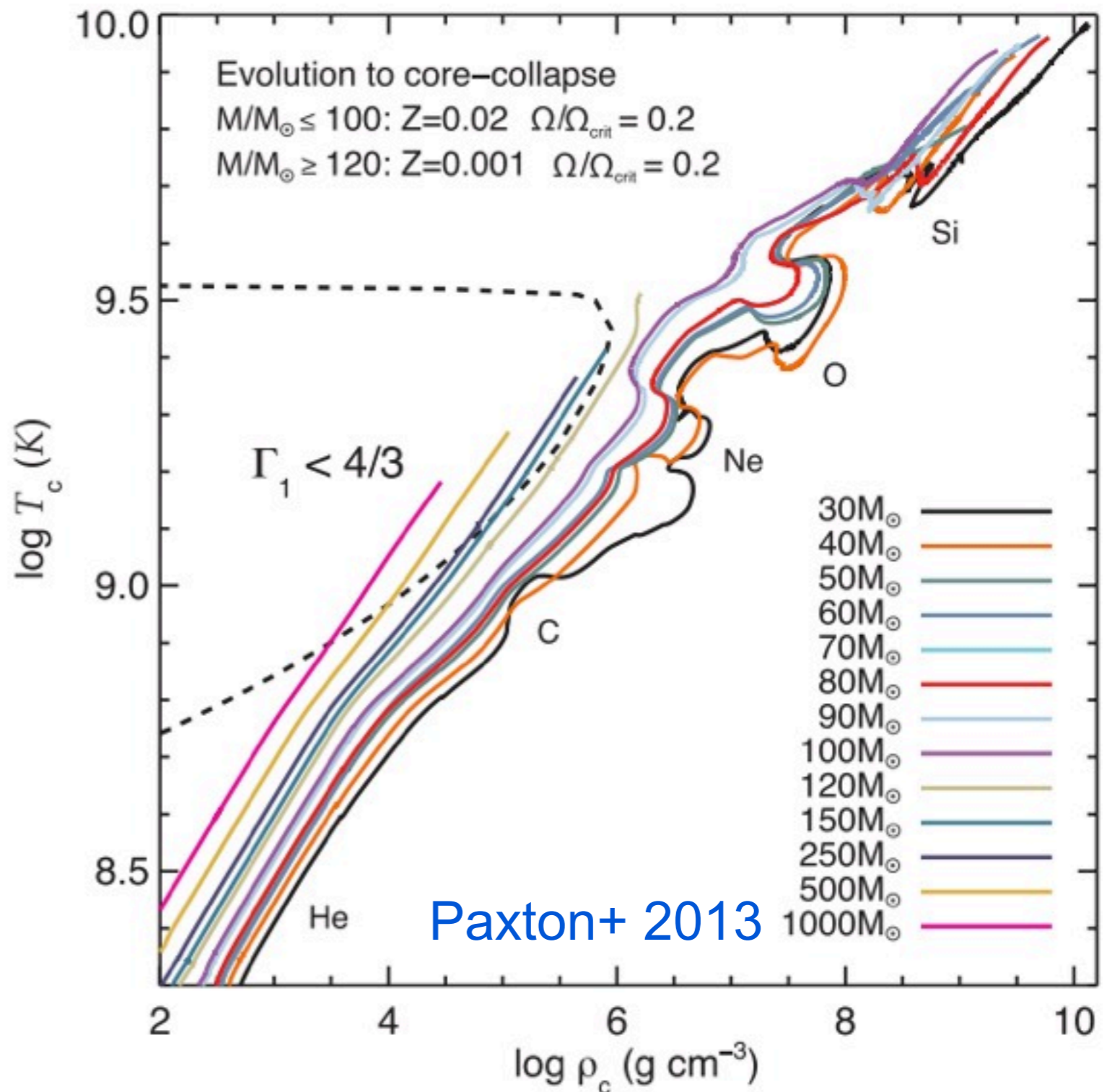
# Early type stars in 30 Doradus



# Stellar Cores

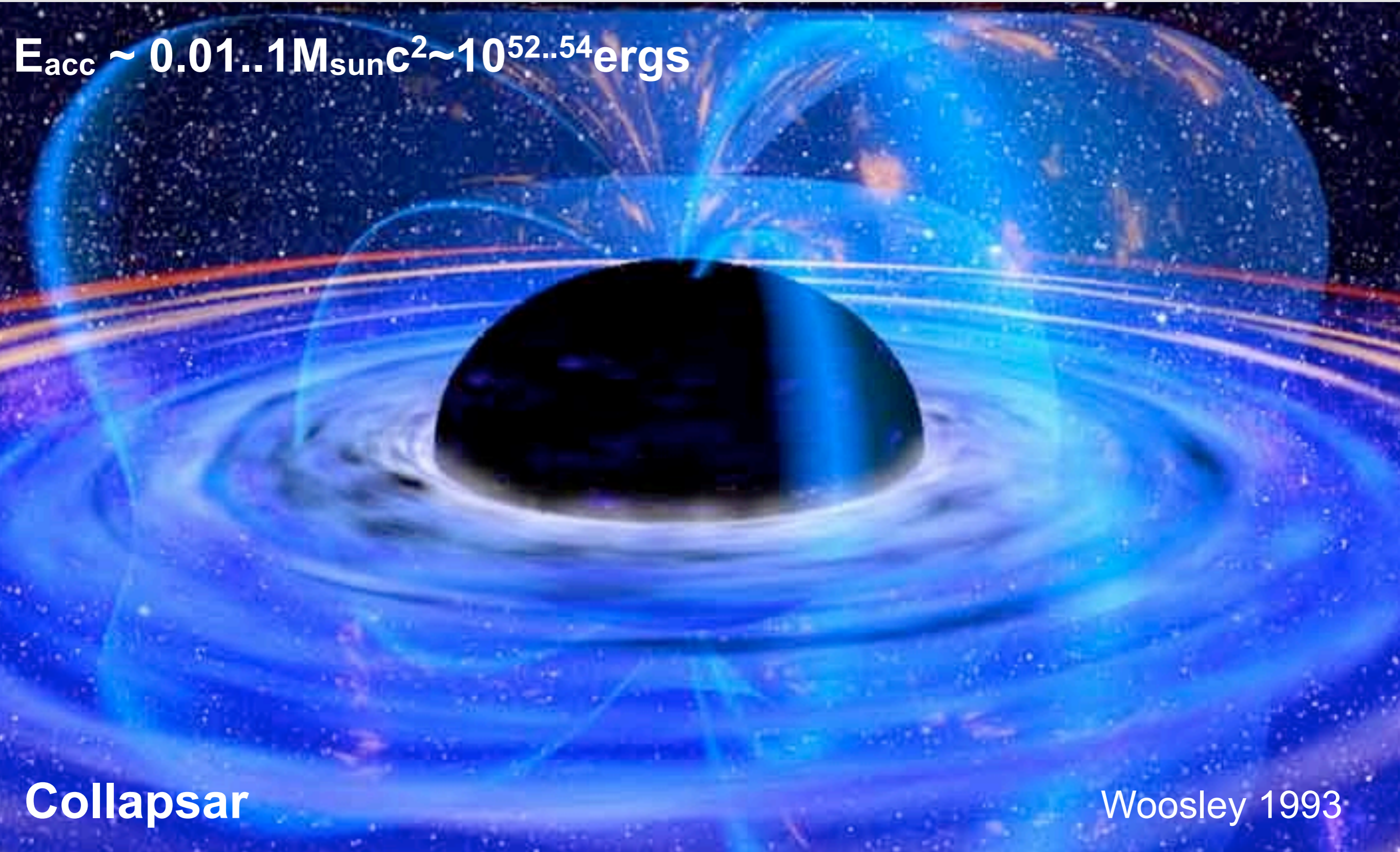
To maintain hydrostatic equilibrium stars need to burn nuclear fuel at higher and higher temperatures. This implies an inexorable **contraction of stellar cores**

In the absence of angular momentum transport mechanisms, stellar cores would **spin up** to very high rotation rates



# Long GRB Central Engine

$E_{\text{acc}} \sim 0.01..1 M_{\text{sun}} c^2 \sim 10^{52..54} \text{ergs}$



**Collapsar**

Woosley 1993

# Long GRB Central Engine

$$E_{\text{rot}} \sim 3 \cdot 10^{52} (P/\text{ms})^{-2} (R/10\text{km})^2 \text{ ergs}$$

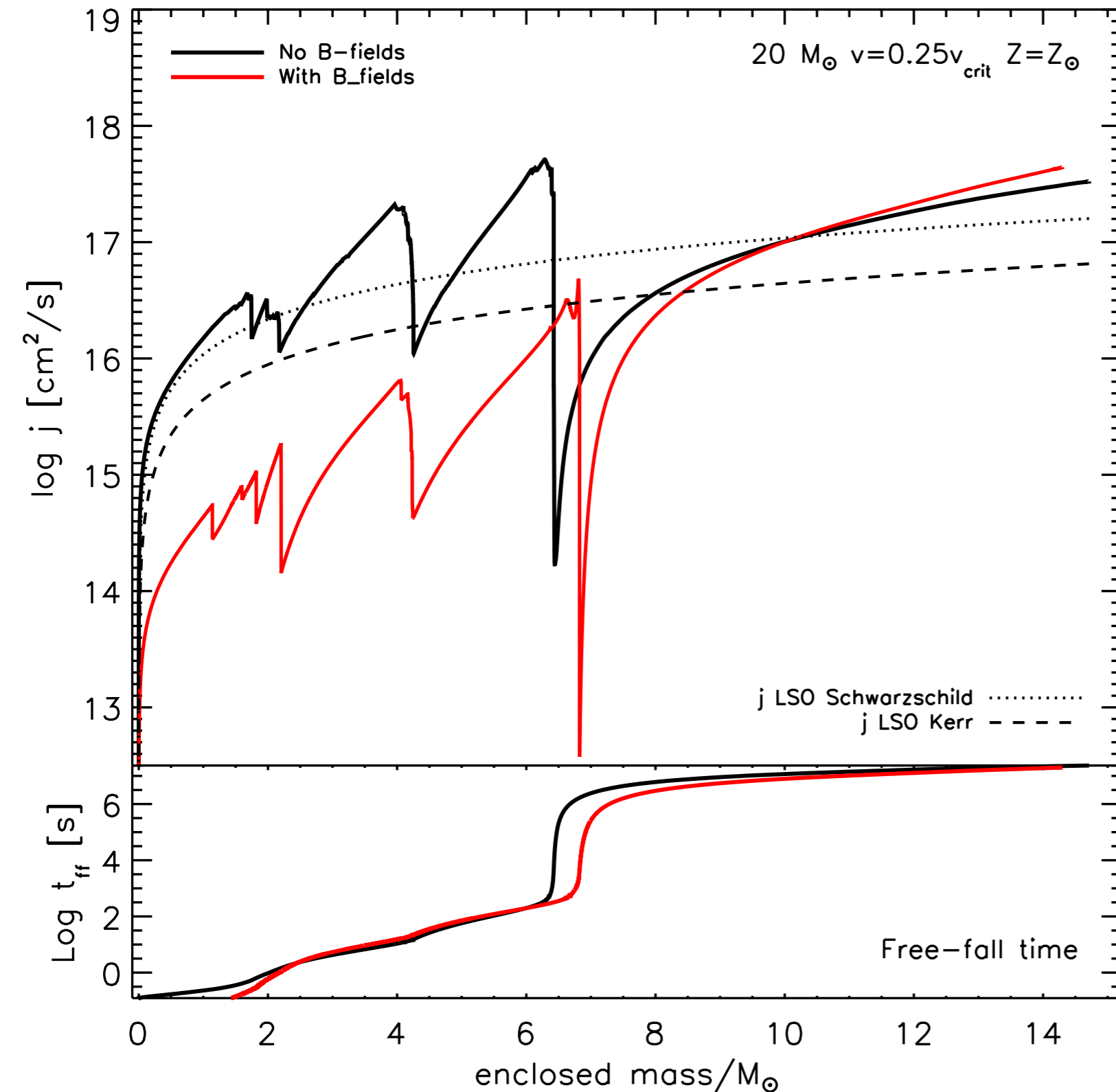
$$\dot{E}_{\text{FF}} \approx \frac{4\pi^4 B_{\text{dip}}^2 R^6}{c^3 P^4} \approx 10^{49} \text{ ergs s}^{-1} \left( \frac{B_{\text{dip}}}{10^{15} \text{G}} \right)^2 \left( \frac{P}{1 \text{ms}} \right)^{-4} \left( \frac{R}{10 \text{km}} \right)^6$$

(Spitkovski 2006)

**Millisecond Magnetar**

Usov 1992

# Final j-distribution



GRB (?): enough angular momentum in the core to make an accretion disk during collapse / create a rapidly rotating NS

SN: no accretion disk during collapse / no rapidly rotating NS

1D **MESA**  
Stellar evolution  
calculations

Paxton+ 2011, 2013, 2015

# Impact of Stellar Rotation

- Internal Mixing
- Mass Loss
- Core Collapse

Overall  
Evolution

Centrifugally  
Enhanced  
Massloss

CC Explosion,  
Central Engines,  
SN Asymmetries,  
Remnants...



# Impact of Stellar Rotation

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See e.g. talks from:

Maria Drout

Ryosuke Hirai

Leah Huk

Jeff Silverman

Laura Chomiuk

# Impact of Stellar Rotation

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Jochen Greiner

Manos Chatzopoulos

Raffaella Margutti

Brian Morsony

William Hix

Bernard Mueller

Remi Kazeroni

Grant Williams

# **Physics of Angular Momentum Transport**

# Timescales & Approximations

$$\tau_{\text{nuc}} \gg \tau_{\text{KH}} \gg \tau_{\text{dyn}}$$

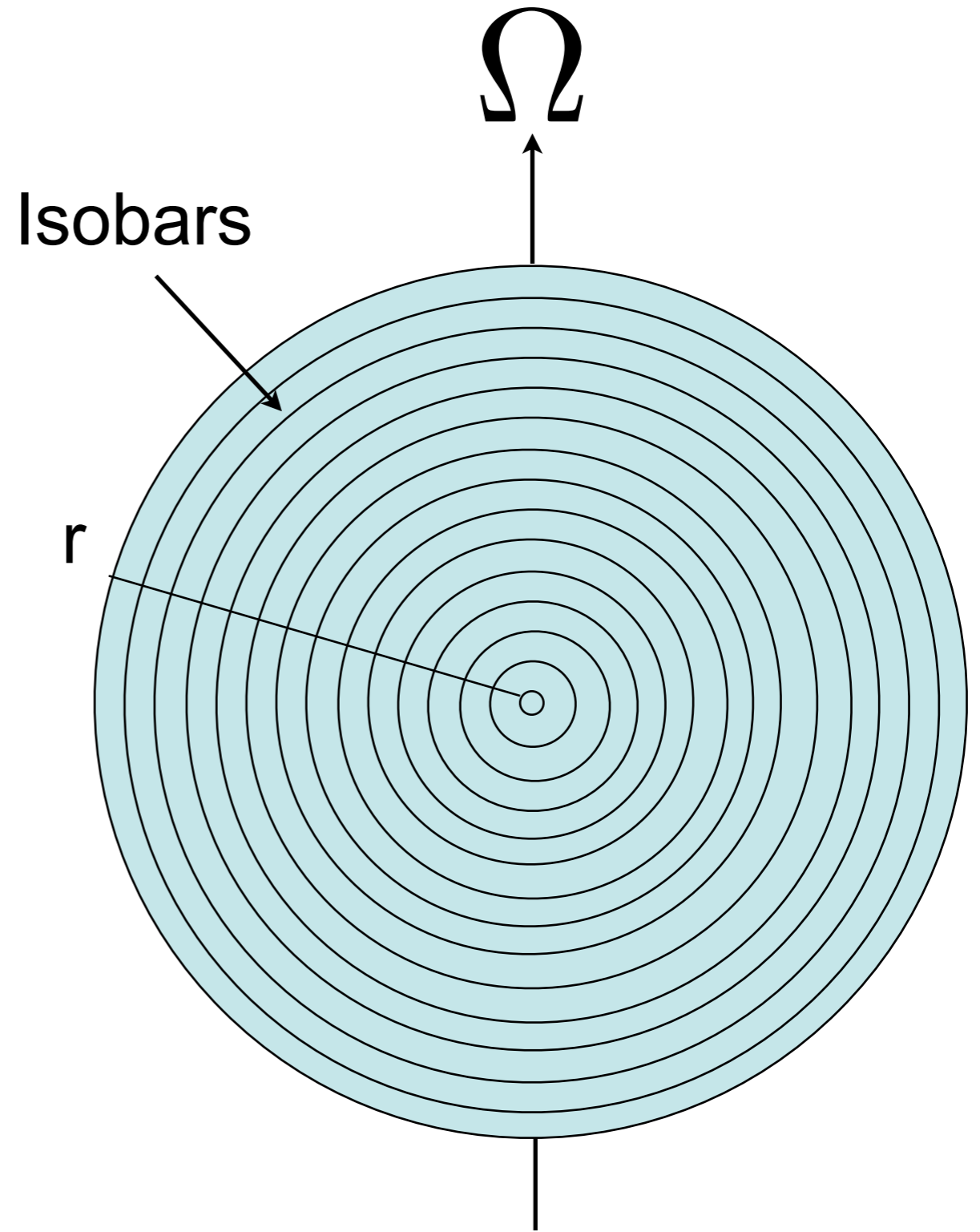
Main Sequence	$t_{\text{nuc}}$	$t_{\text{KH}}$	$t_{\text{dyn}}$
1 $M_{\text{Sun}}$	$10^{10}$ yr	$10^7$ yr	0.02 d
10 $M_{\text{Sun}}$	$\sim 10^7$ yr	$10^4$ yr	0.1 d
100 $M_{\text{Sun}}$	$\sim 10^6$ yr	$10^3$ yr	0.5 d

To resolve and include dynamical phenomena one has to take  $\sim 10^{11}$  timesteps. This is beyond current capabilities. Stellar evolution requires **MLT**, **Diffusion approximations** etc.

# Rotation in 1D: The Shellular Approximation

$$\omega = \omega(r)$$

Composition is only function of the  $r$  coordinate, as each shell is assumed to be efficiently mixed by strong horizontal turbulence

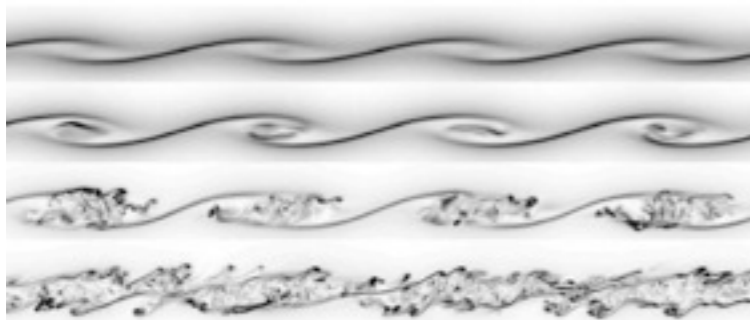


Zahn (1975), Chaboyer & Zahn (1992), Meynet & Maeder 1997

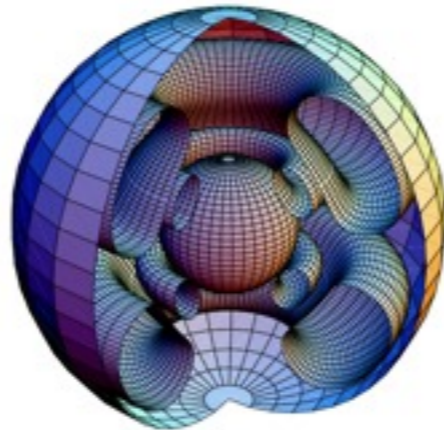
# Angular Momentum Transport

Different classes of mechanisms have been proposed:

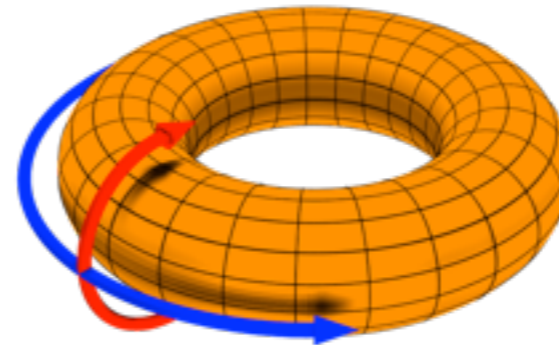
e.g. Heger et al. 2000



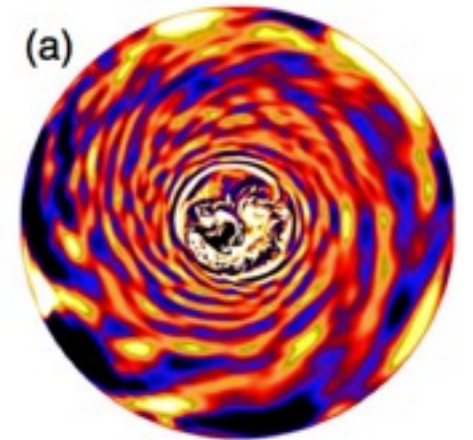
e.g. Maeder & Meynet 2002



e.g. Spruit 2002



e.g. Rogers et al. 2013



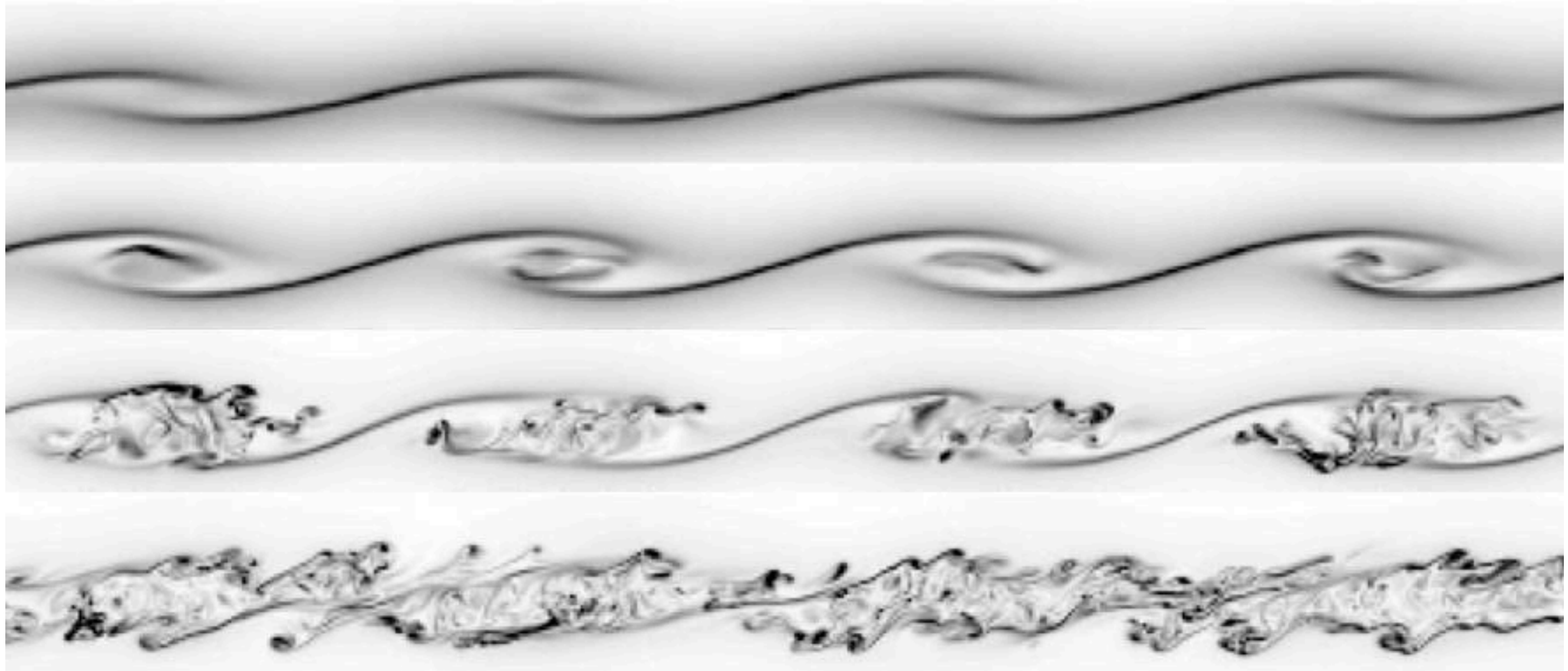
- **Hydrodynamics instabilities**
- **Rotationally induced circulations**
- **Magnetic torques**
- **Internal gravity waves**

Convective Regions usually assumed rigidly rotating

# Hydrodynamic Instabilities

## ■ Dynamical Shear

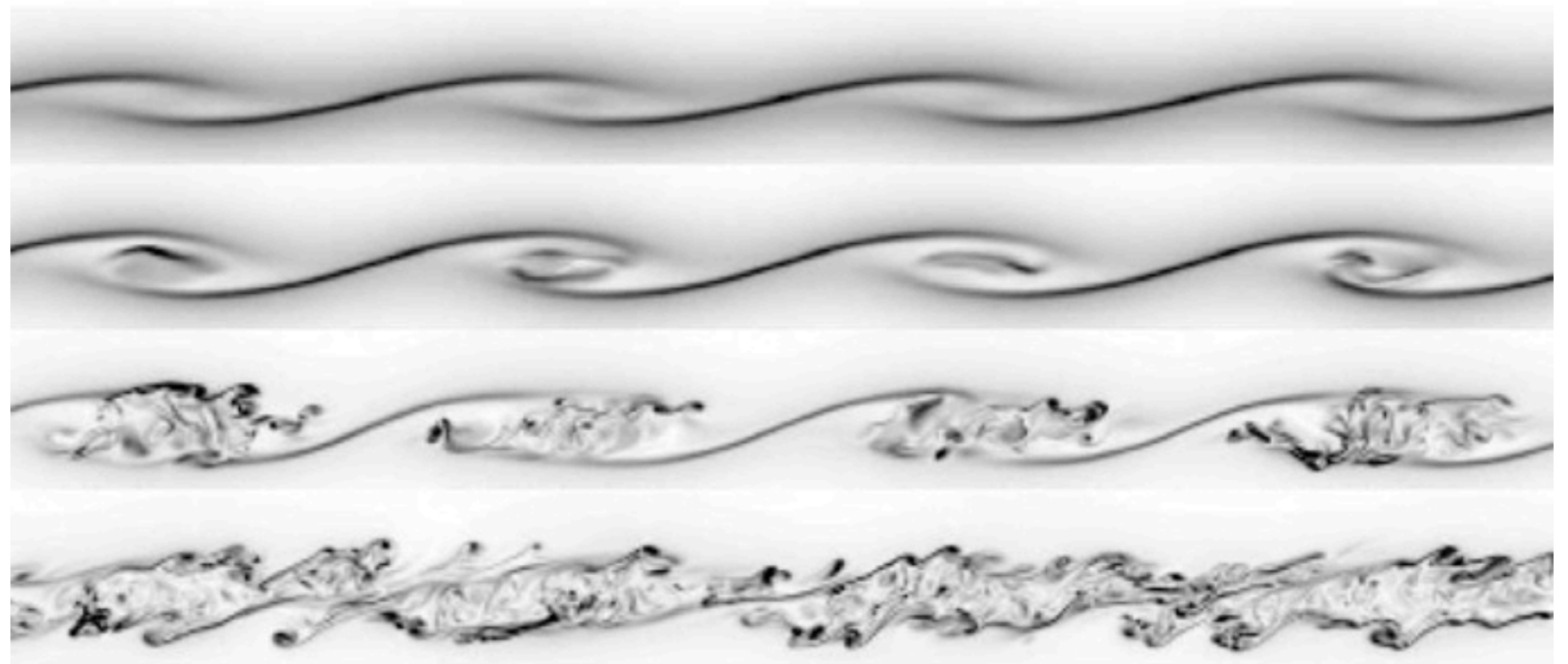
Dynamical shear instability occurs when the energy that can be gained from the shear flow becomes comparable to the work that has to be done against the gravitational potential for the adiabatic turnover of a mass element



# Hydrodynamic Instabilities

## ■ Secular Shear

Thermal  
Timescale



■ In the presence of a stabilizing thermal gradient, an eddy might have to wait for heat to diffuse out before an overturn is energetically favorable

■ Mixing process on  $t_{KH}$

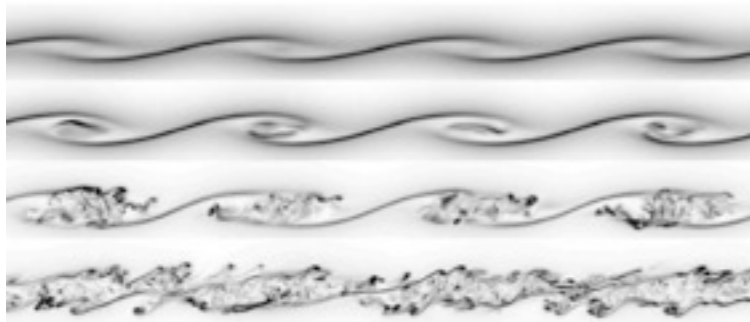
More Hydro instabilities:  
see e.g. [Heger et al. 2000](#)



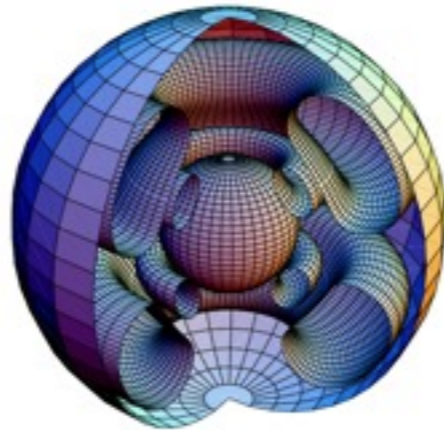
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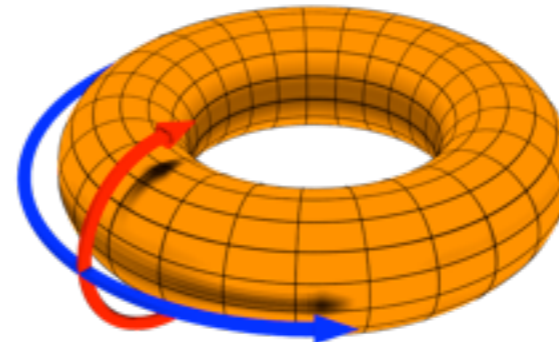
e.g. Heger et al. 2000



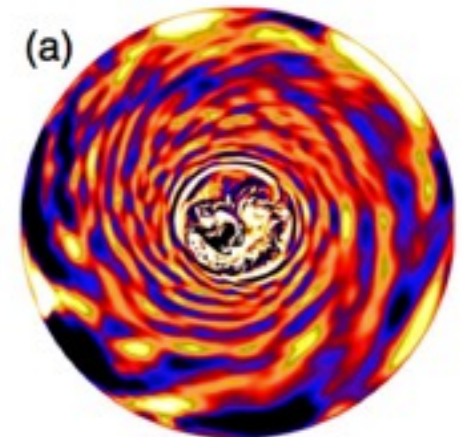
e.g. Maeder & Meynet 2002



e.g. Spruit 2002



e.g. Rogers et al. 2013



- Hydrodynamics instabilities
- **Rotationally induced circulations**
- Magnetic torques
- Internal gravity waves

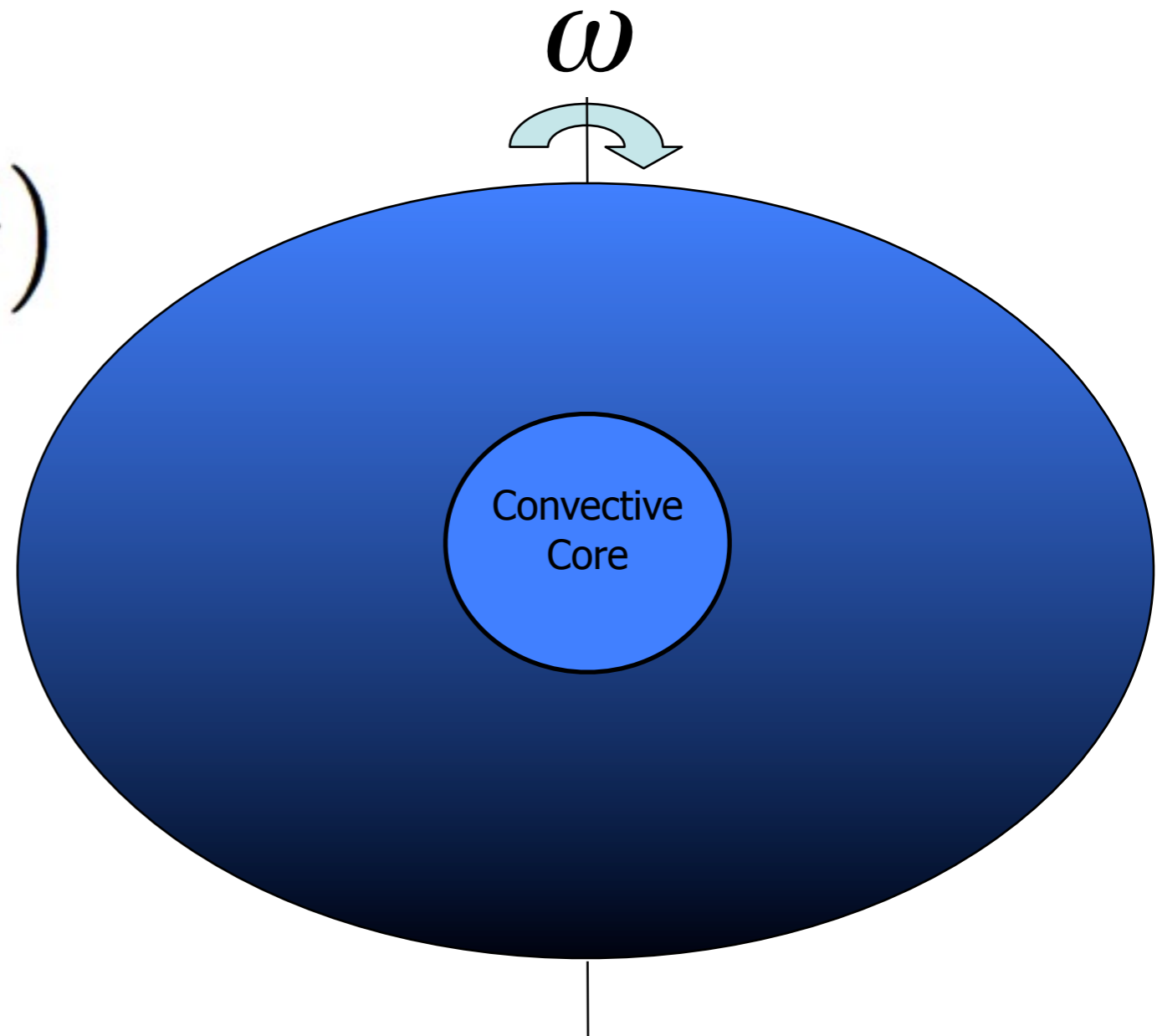
# Rotationally Induced Circulations

The thermal flux through the surface of a (radiative) rotating star is proportional to the local effective gravity. Since this depends on the co-latitude, one expects a greater radiative flux at the poles than at the equator.

$$T_{\text{eff}}(\vartheta) \sim g_{\text{eff}}^{1/4}(\vartheta)$$

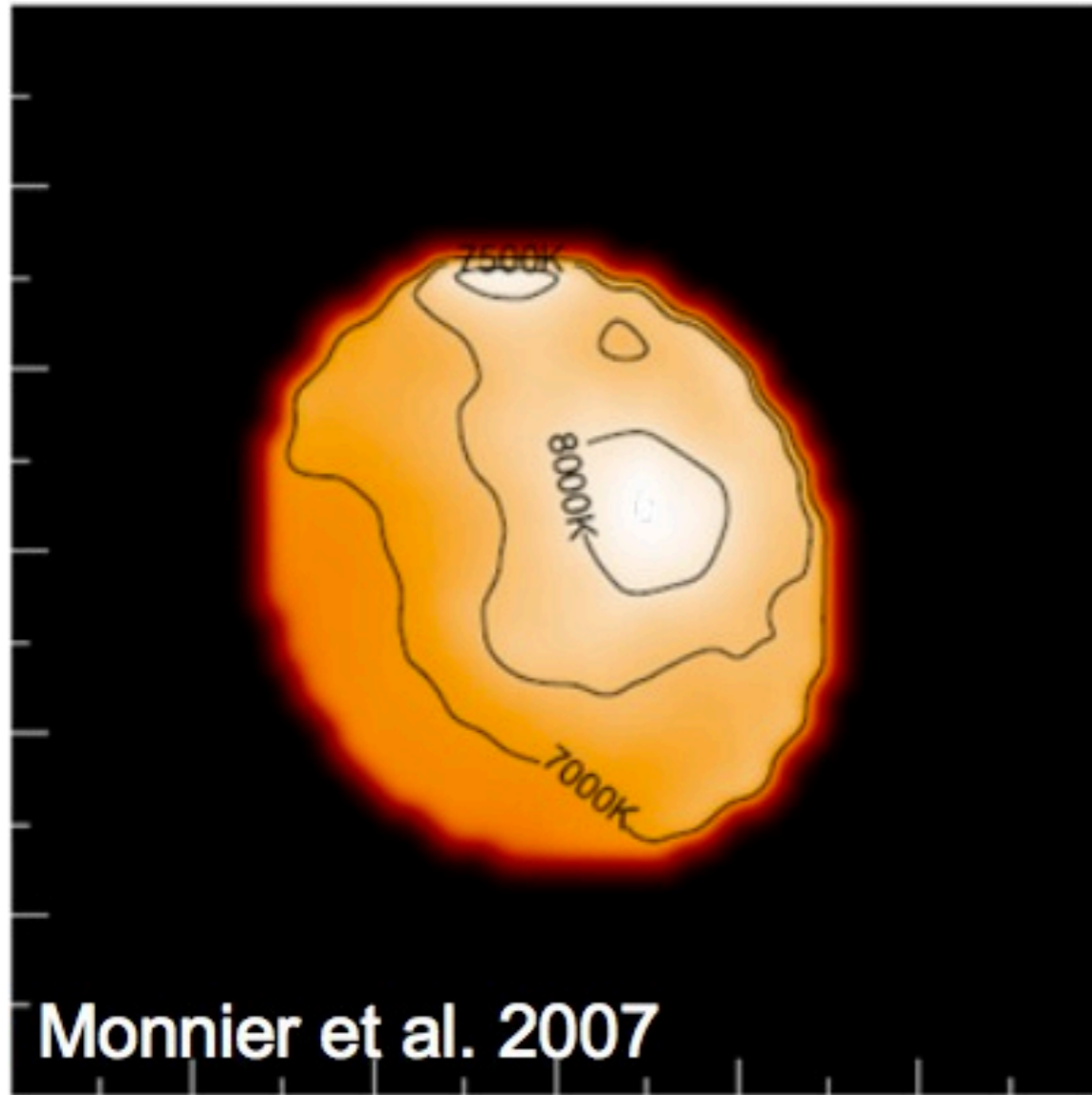
## Von Zeipel Theorem

Von Zeipel (1924)

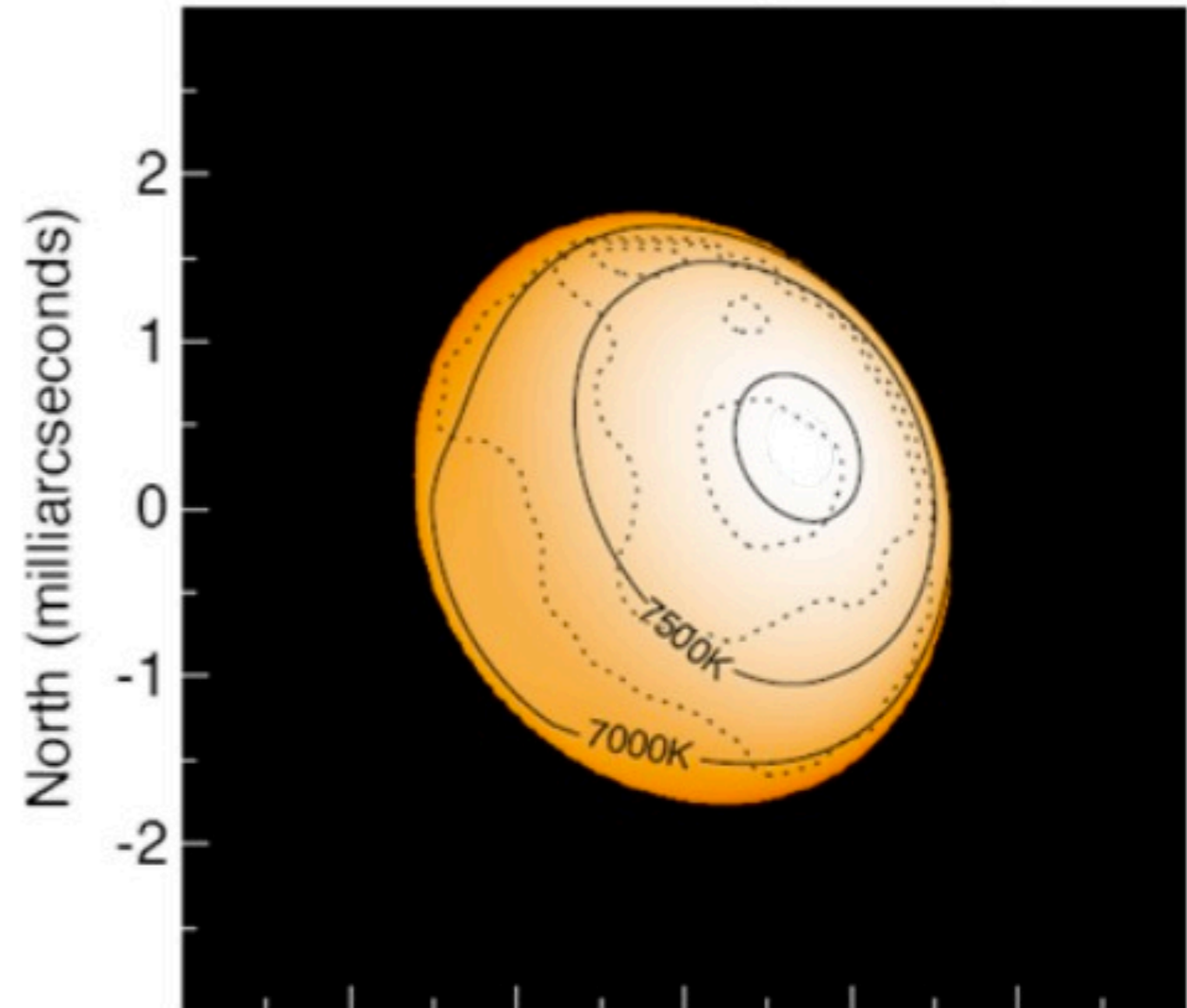


# Interferometry of rotating stars

Altair Image Reconstruction

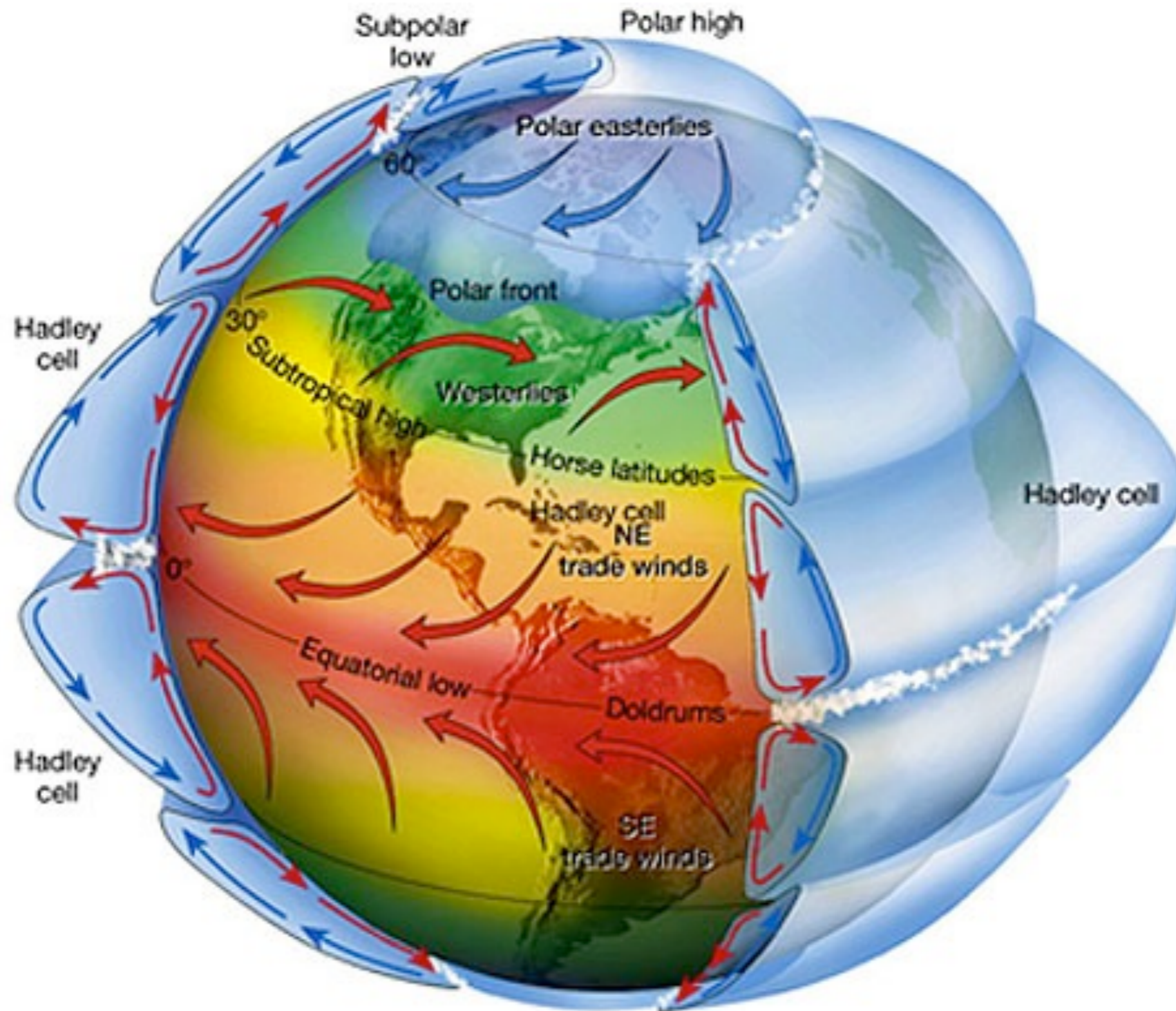


Altair Model ( $\beta=0.19$ )



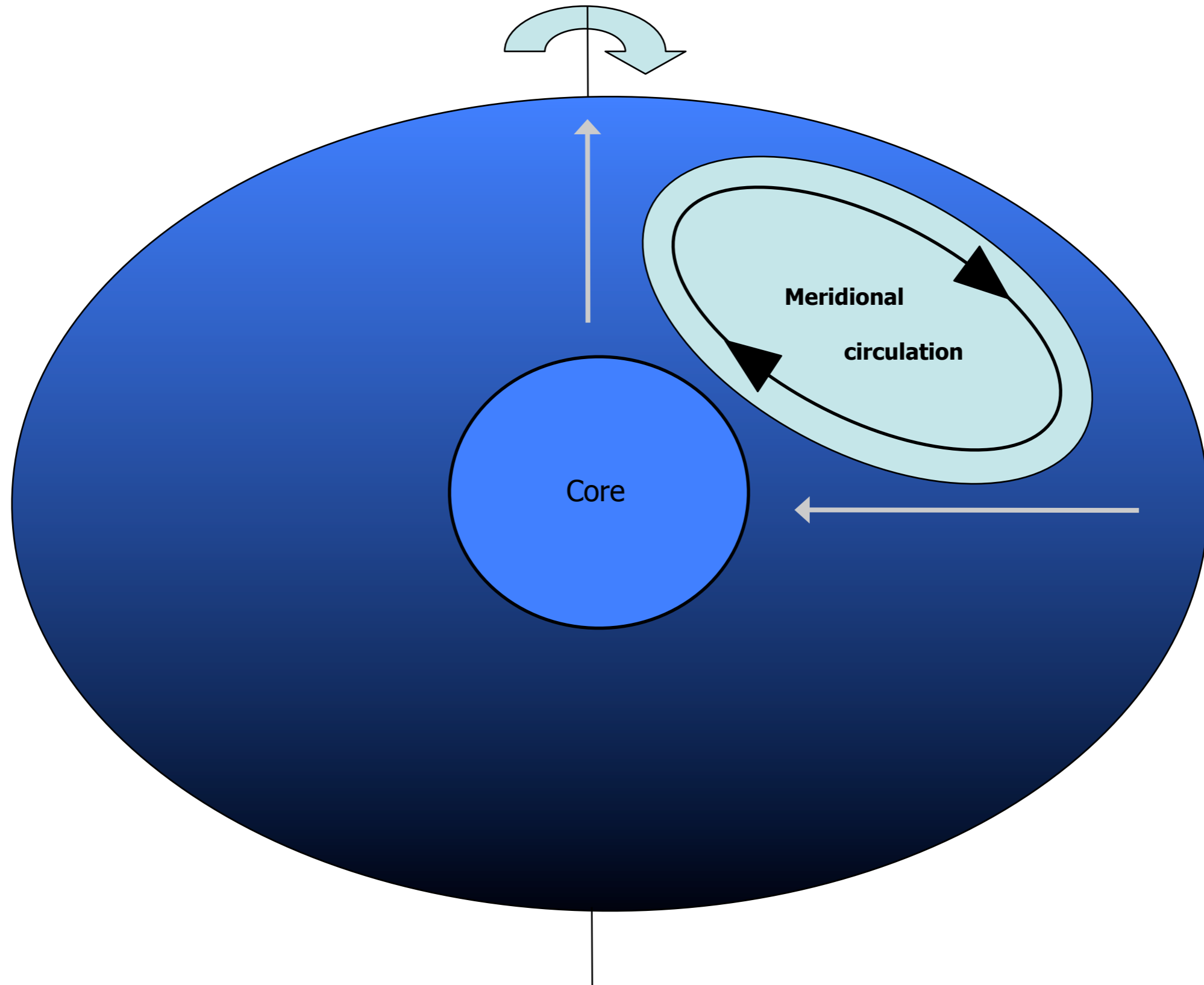
**Altair (A7IV-V Star):** confirms Von Zeipel 'gravity darkening' even if with a slightly different exponent

# Thermal imbalance drives circulations



# Thermal imbalance drives circulations

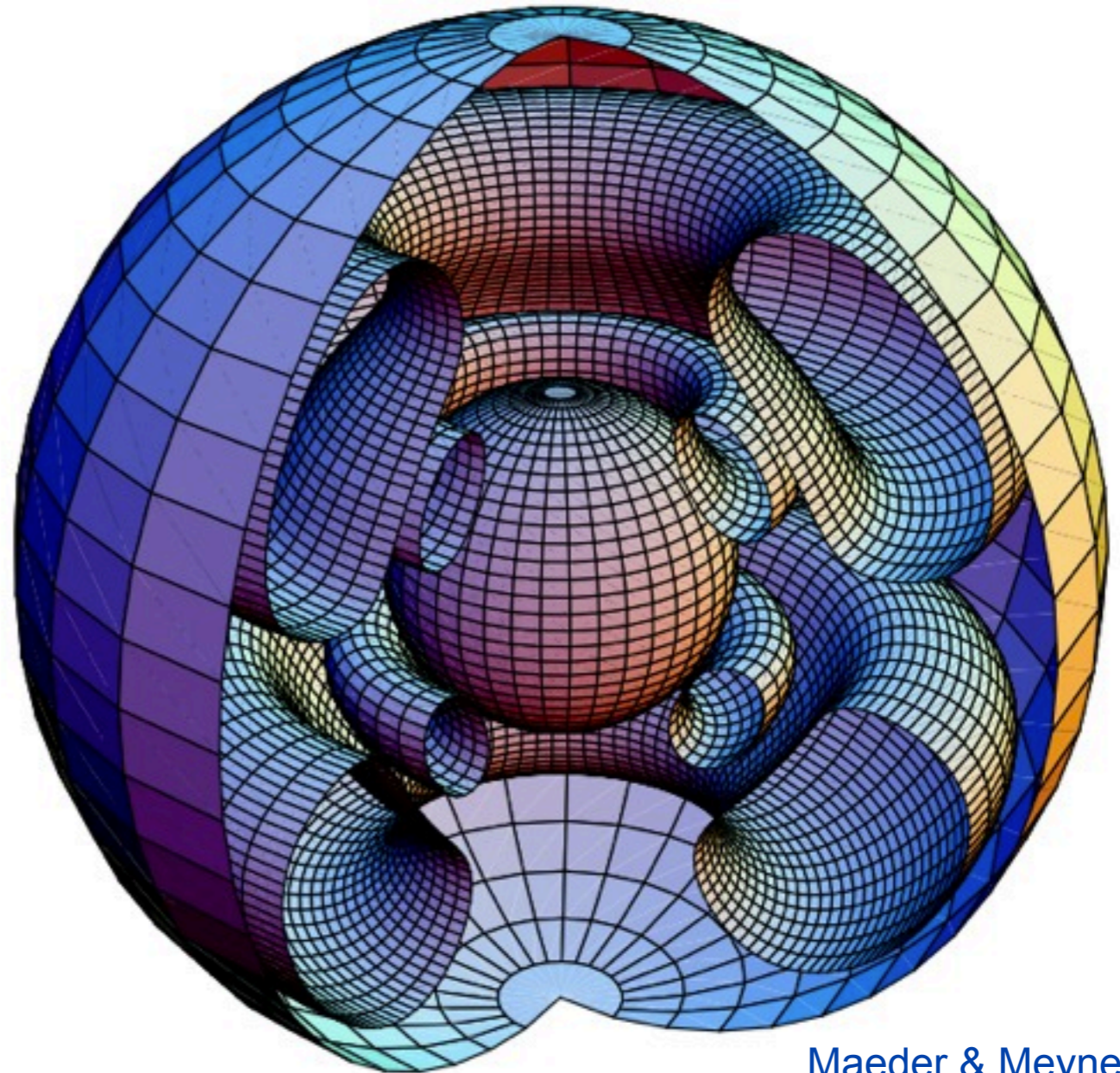
# Thermal imbalance drives circulations



# Rotationally Induced Circulations

- **Eddington-Sweet Circulation**
- Is a meridional circulation mixing the stellar interior
- Mixing process on  $t_{KH}$

$$\tau_{ES} \propto \tau_{KH} \left( \frac{\omega_K}{\omega} \right)^2$$

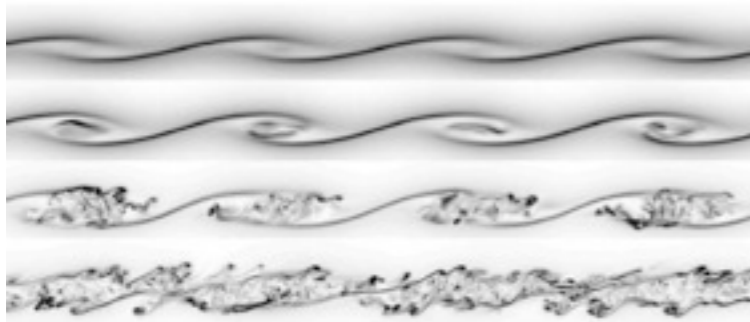


Maeder & Meynet 2002

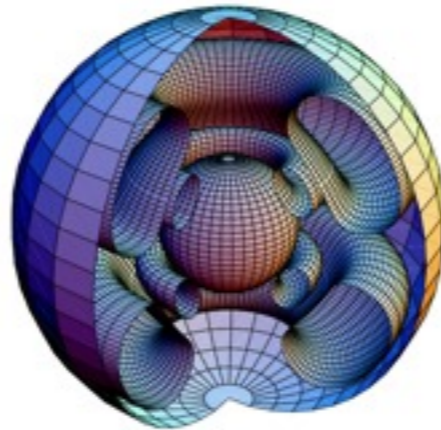
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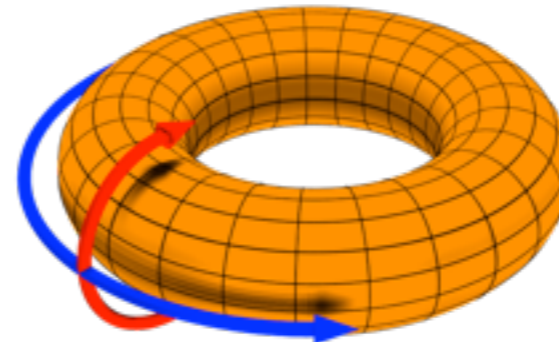
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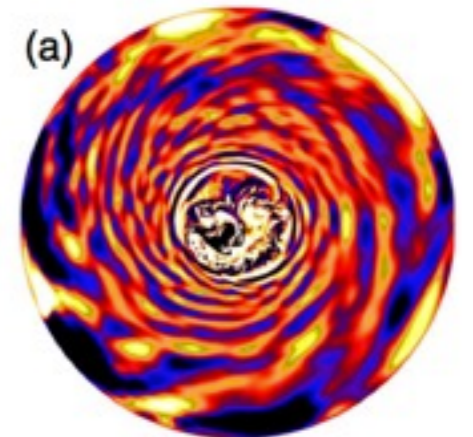
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e.g. Spruit 2002



e.g. Rogers et al. 2013



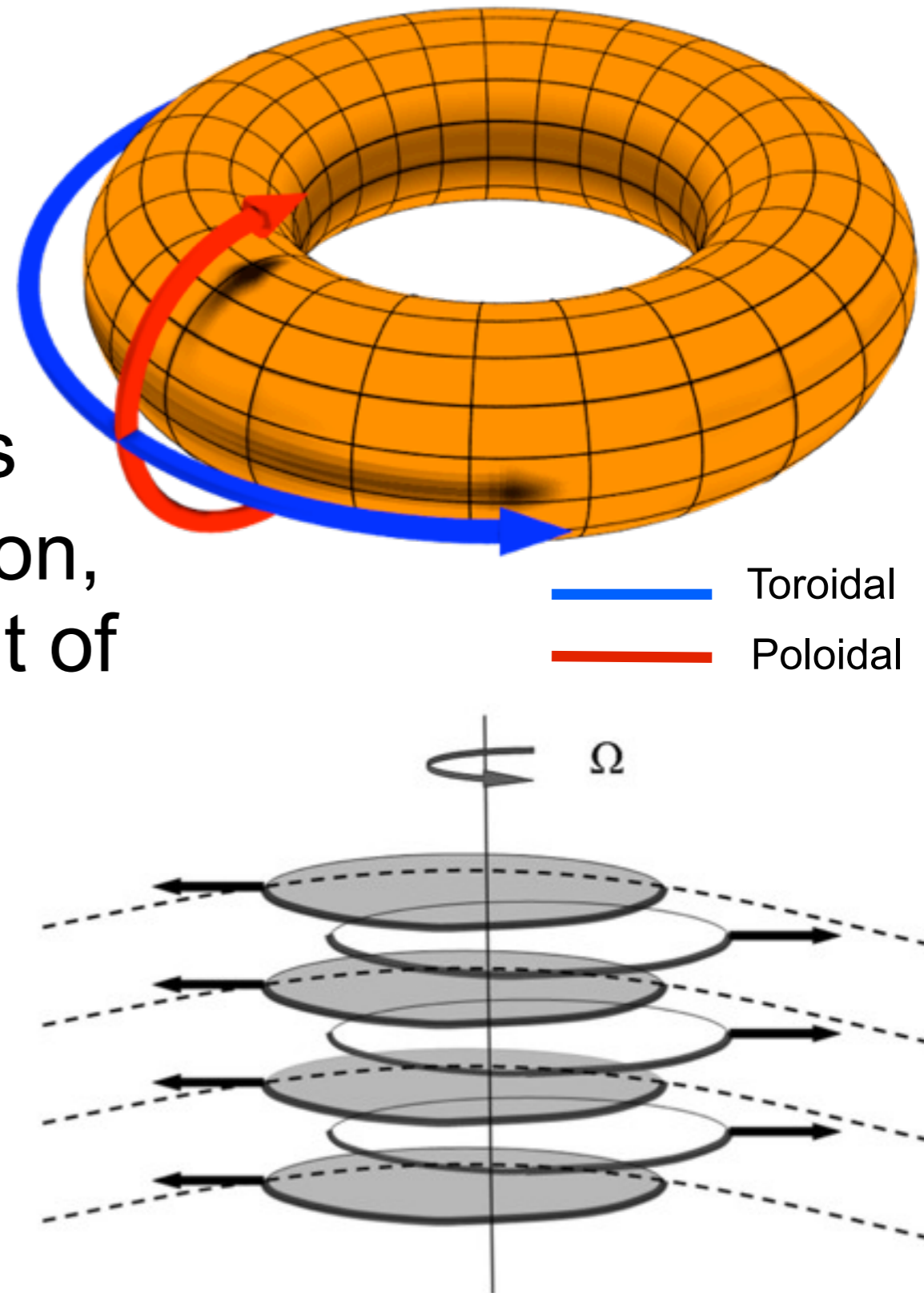
- Hydrodynamics instabilities
- Rotationally induced circulations
- **Magnetic torques**
- Internal gravity waves



# Taylor-Spruit Dynamo

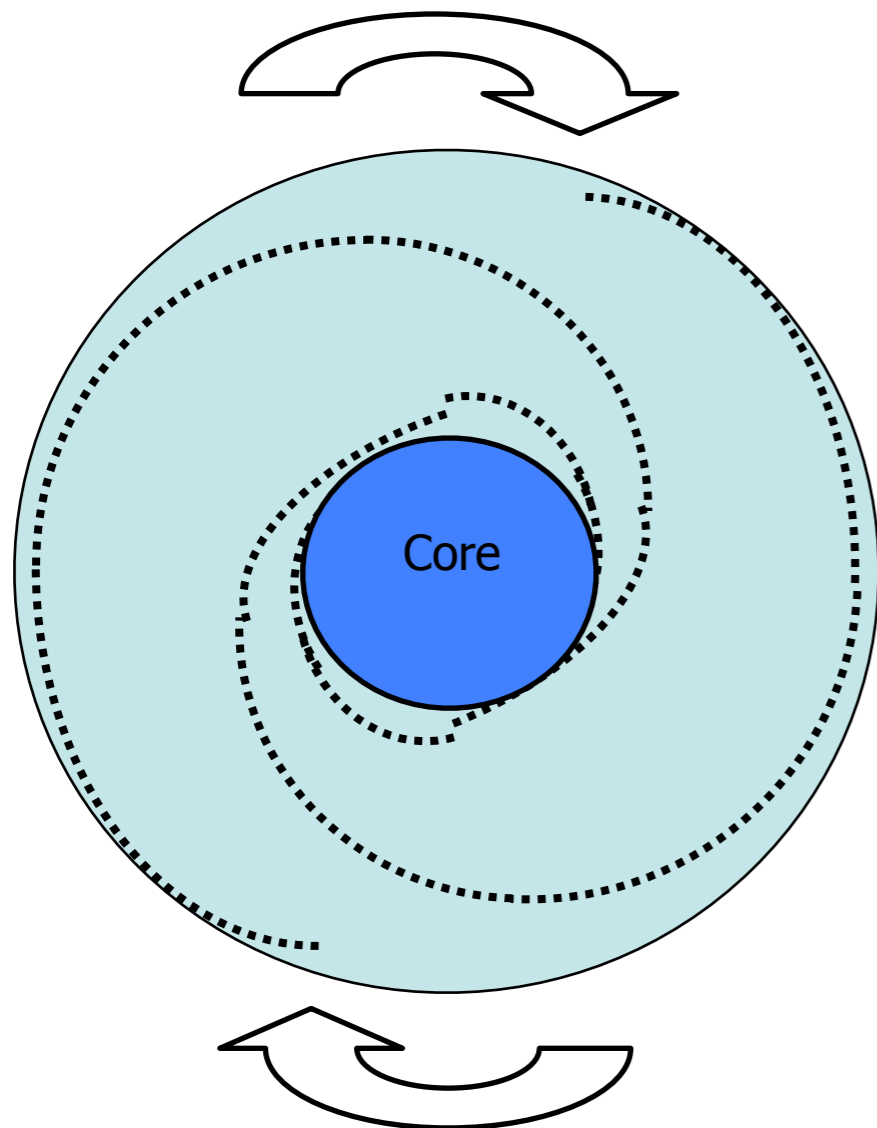
- Dynamo in a radiative layer
- Magnetic energy is generated from differential rotation
- Initially a seed magnetic field is stretched by the differential rotation, amplifying the toroidal component of the field
- An instability in the toroidal component of the field (Taylor instability) is used to close the dynamo loop

Spruit 2002

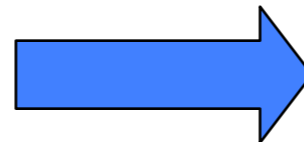


# Taylor-Spruit Dynamo

- Taylor-Spruit Dynamo ([Spruit 2002](#))
- Core - Envelope coupling



1. Differential rotation winds up toroidal component of  $B$
2. Magnetic torques tend to restore rigid rotation



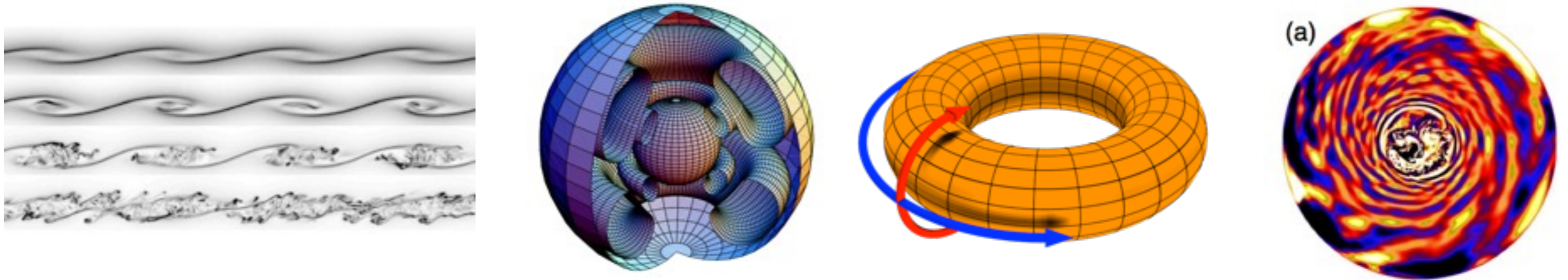
If the envelope slows down angular momentum is also removed from the core

# Debate on the TS Dynamo

- The Tayler-Spruit (TS) dynamo is still under review
- While the Tayler instability is sound, the loop proposed by Spruit has been criticized
- Simulations of [Zahn et al. 2007](#) could not find dynamo action
- On the other hand simulations of [Braithwaite et al. 2006](#) showed the TS dynamo
- The jury is still out, but it looks like a j-transport mechanism similar (or even more efficient, see later) than the TS has to work in stars to reproduce some observations (e.g. spin rates of compact remnants, solar rotation profile, Red Giants core rotation) [Suijs et al. 2008](#), [Eggenberger et al. 2005](#), [Cantiello et al. 2014](#)

# Angular Momentum Transport

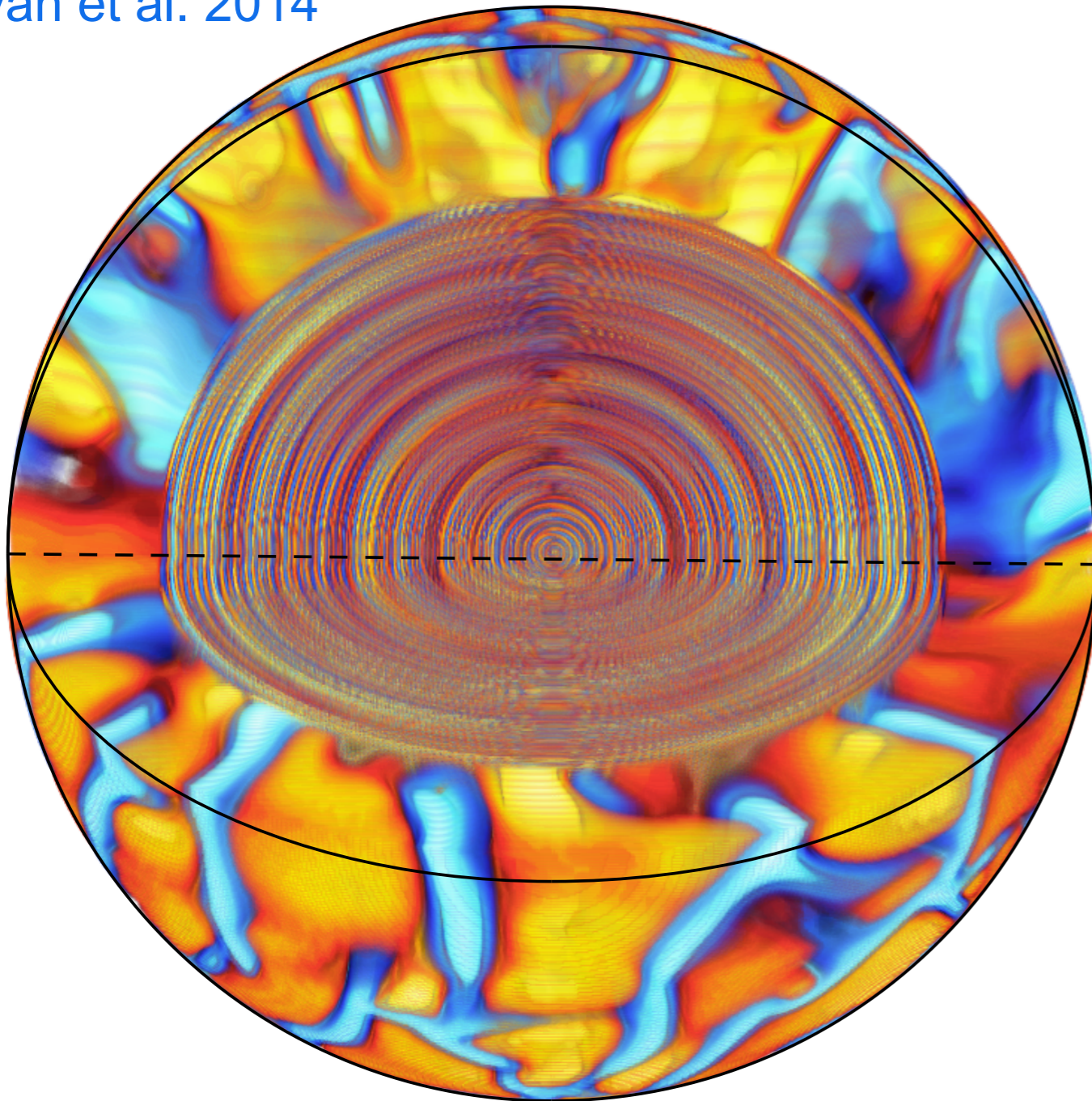
Different classes of mechanisms have been proposed:



- Hydrodynamics instabilities
- Rotationally induced circulations
- Magnetic torques
- **Internal gravity waves**
  - Charbonnel & Talon 2005
  - Rogers et al. 2013
  - Alvan et al. 2014
  - Fuller, Lecoanet, MC et al. 2014
  - Fuller, MC et al. 2015

# Internal Gravity Waves

Alvan et al. 2014



**IGW:** Excited by turbulent convection

**They carry angular momentum**

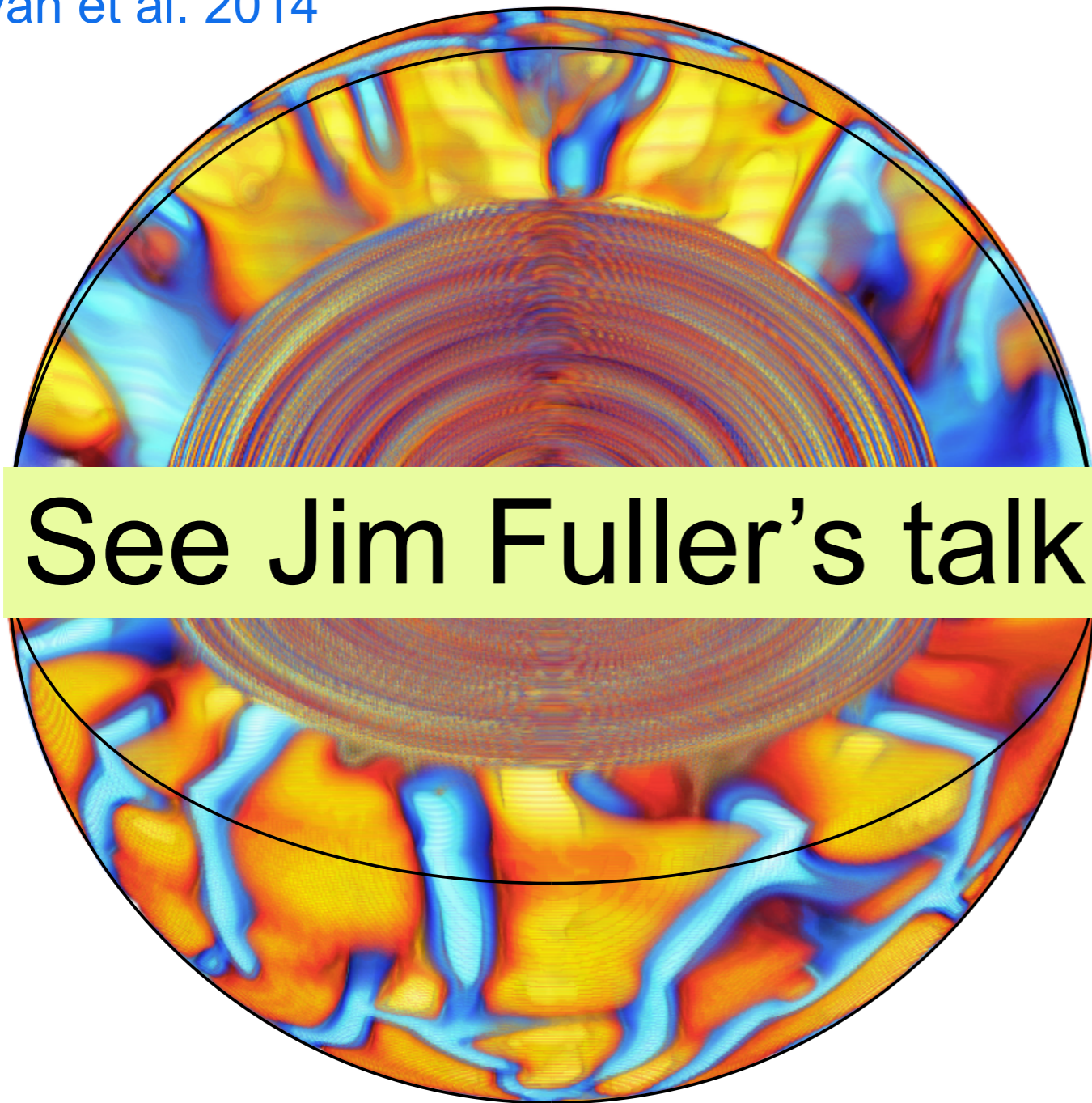
**Spectrum:** Not well understood. But likely Kolmogorov-like with a steep exponent

**Dissipation:** Radiative dissipation usually dominates in stellar interiors

See e.g.: Charbonnel & Talon 2005, Goldreich & Kumar 1990, Lecoanet & Quatert 2013, Mathis et al. 2014, Rogers et al. 2013, Fuller, MC et al. 2015

# Internal Gravity Waves

Alvan et al. 2014



See Jim Fuller's talk

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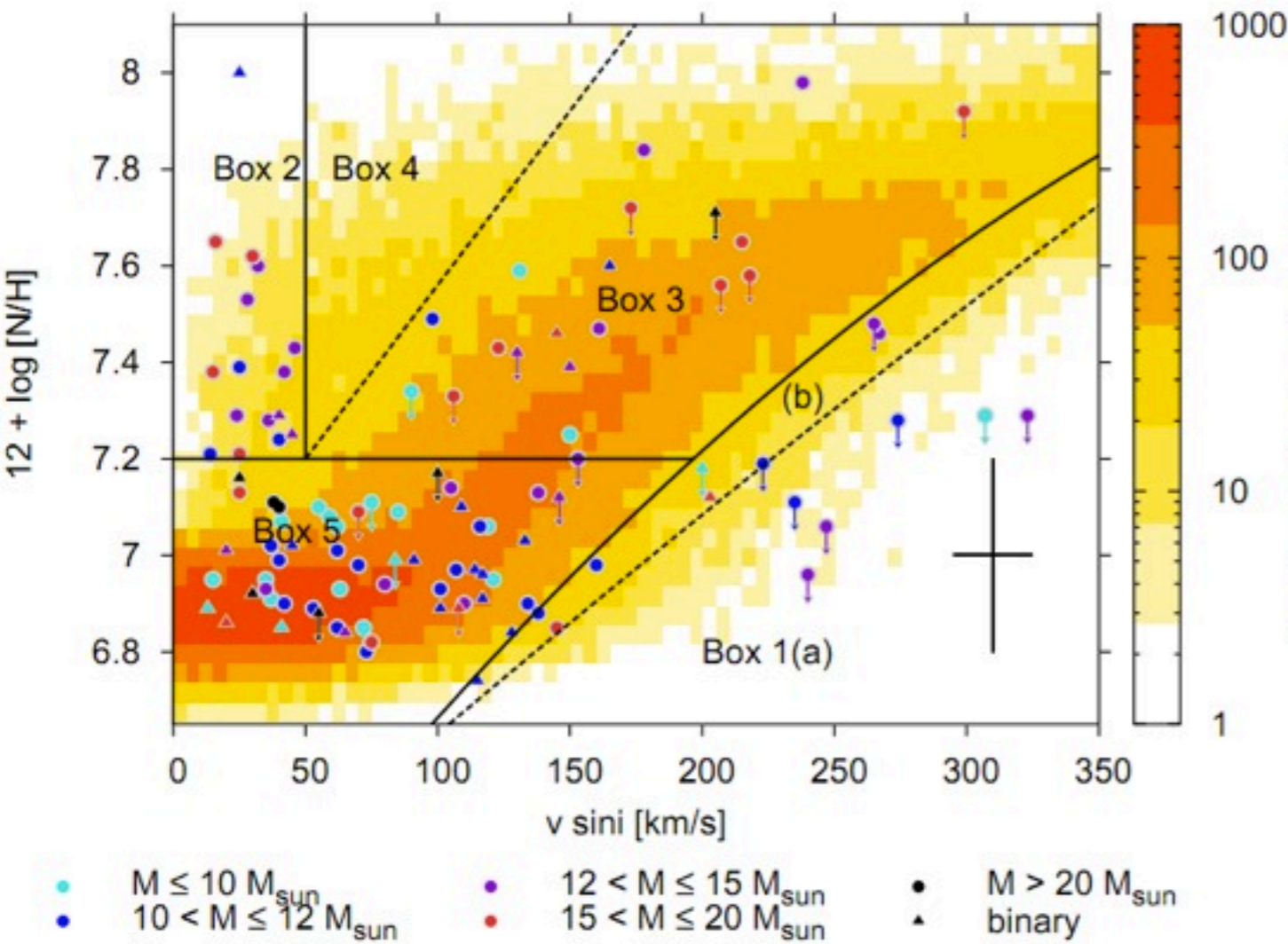
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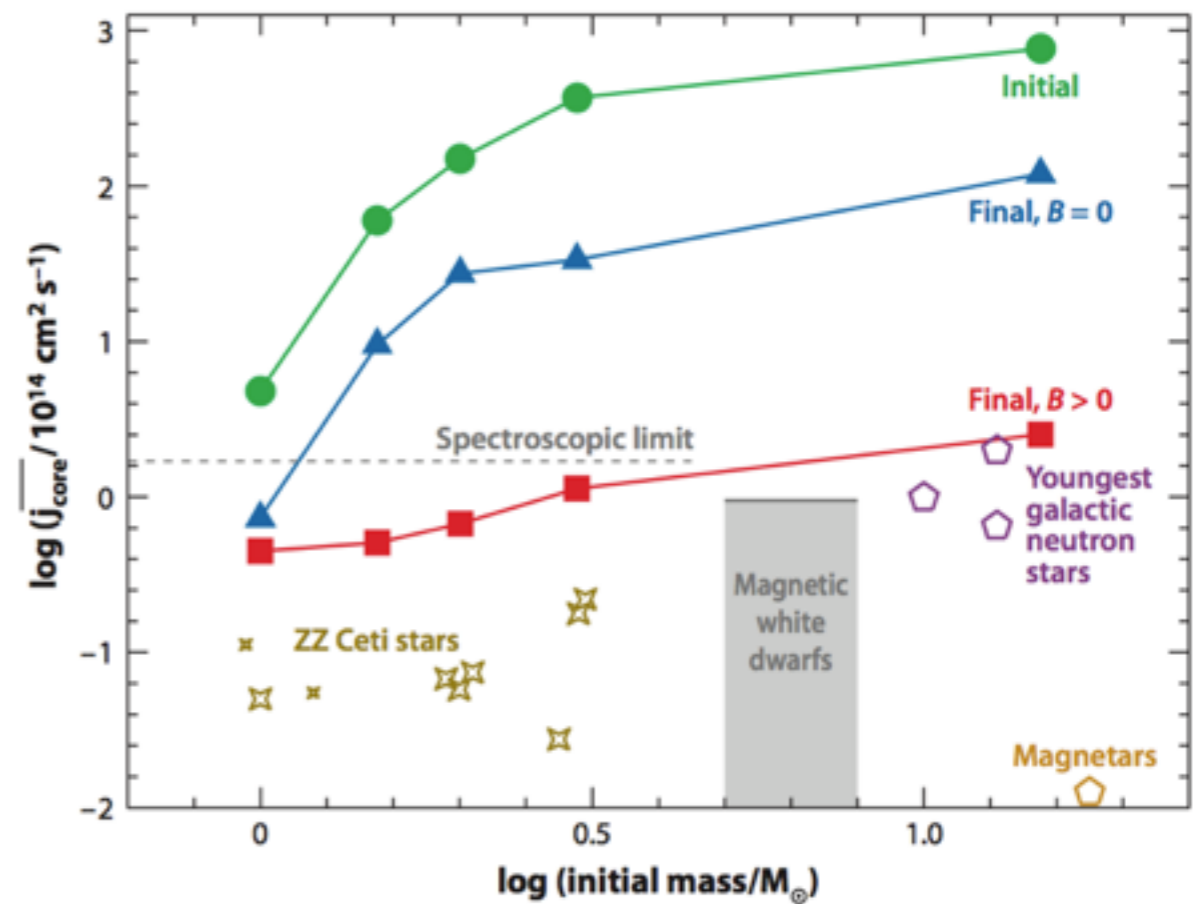
# **Tests of Angular Momentum Transport**

# Testing angular momentum transport mechanisms

Brott et al. 2011



Suijs et al. 2008

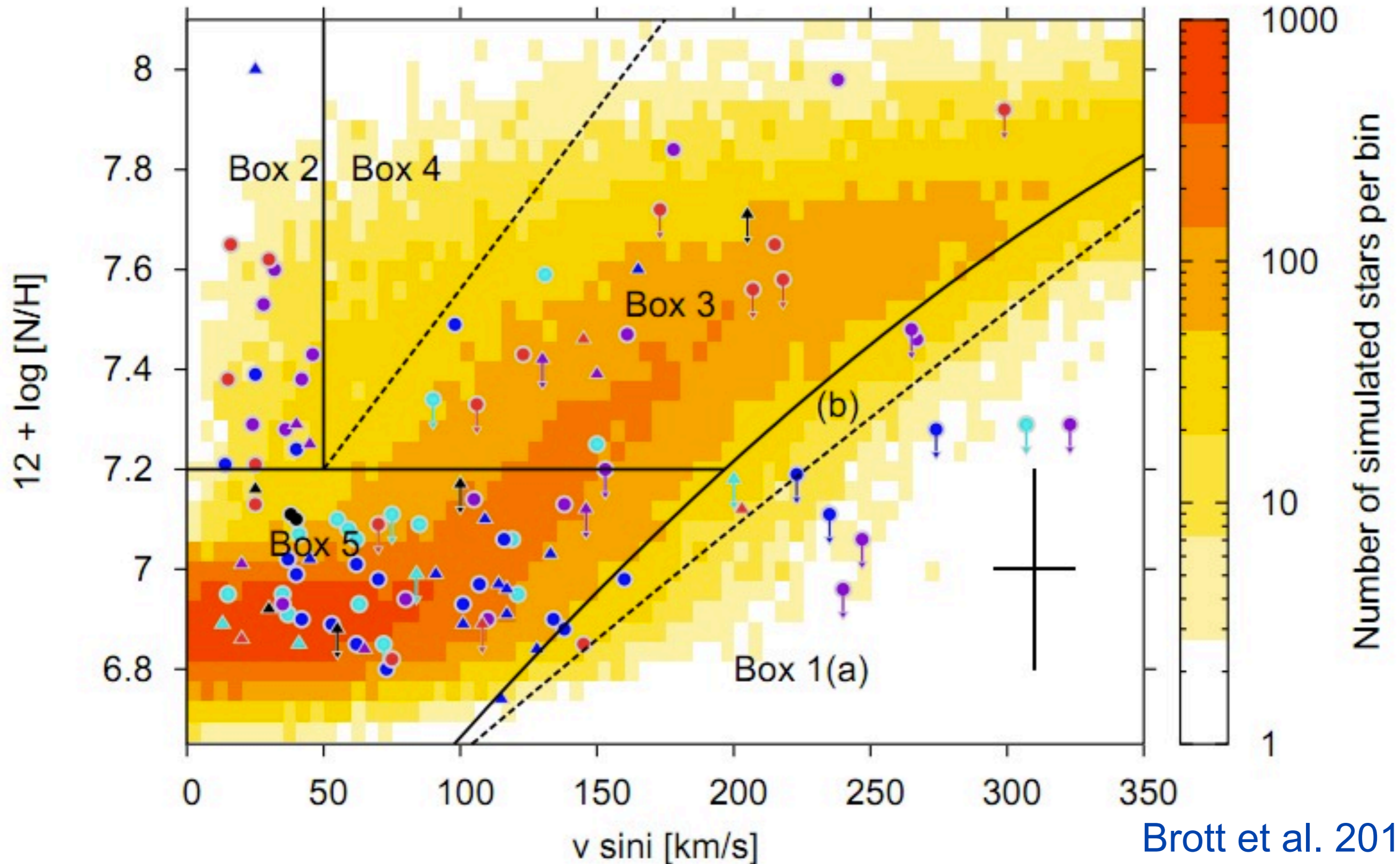


■ Surface abundances

■ Compact Remnants

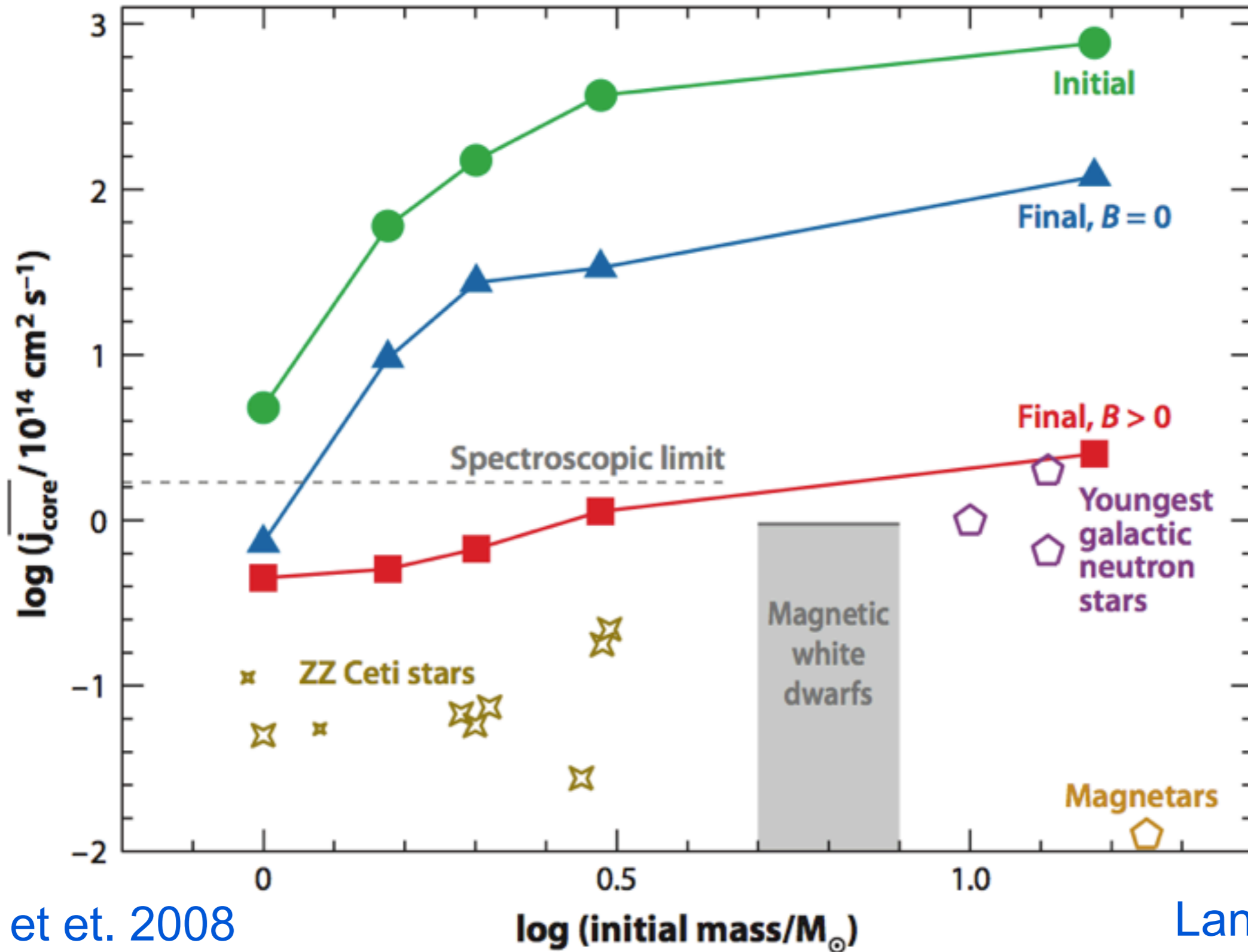


# Testing angular momentum transport mechanisms



Brott et al. 2011

# Testing angular momentum transport mechanisms



Suijs et al. 2008

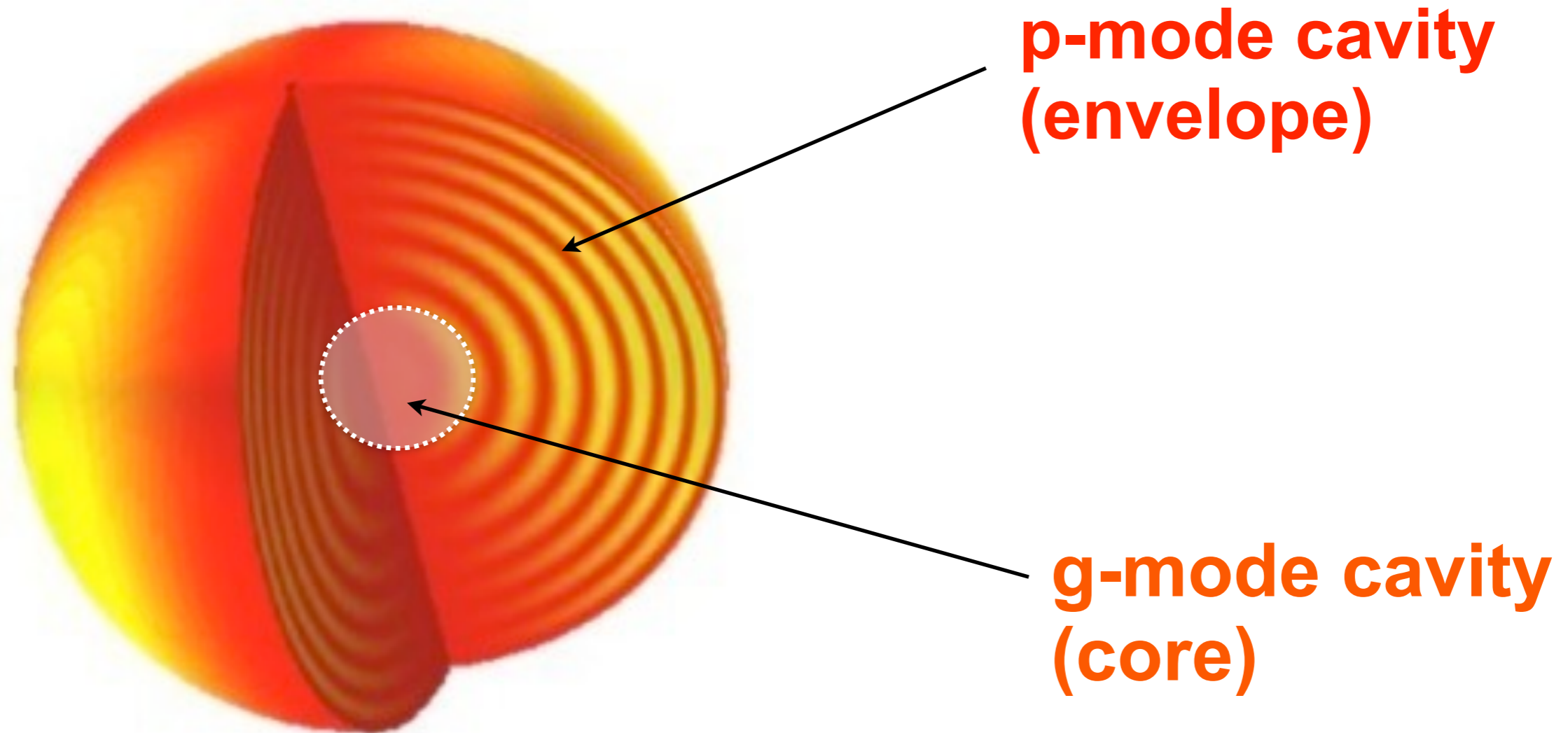
Langer 2012

# Testing angular momentum transport mechanisms

- Surface abundances
- Rotation of compact remnants
- **Asteroseismology**

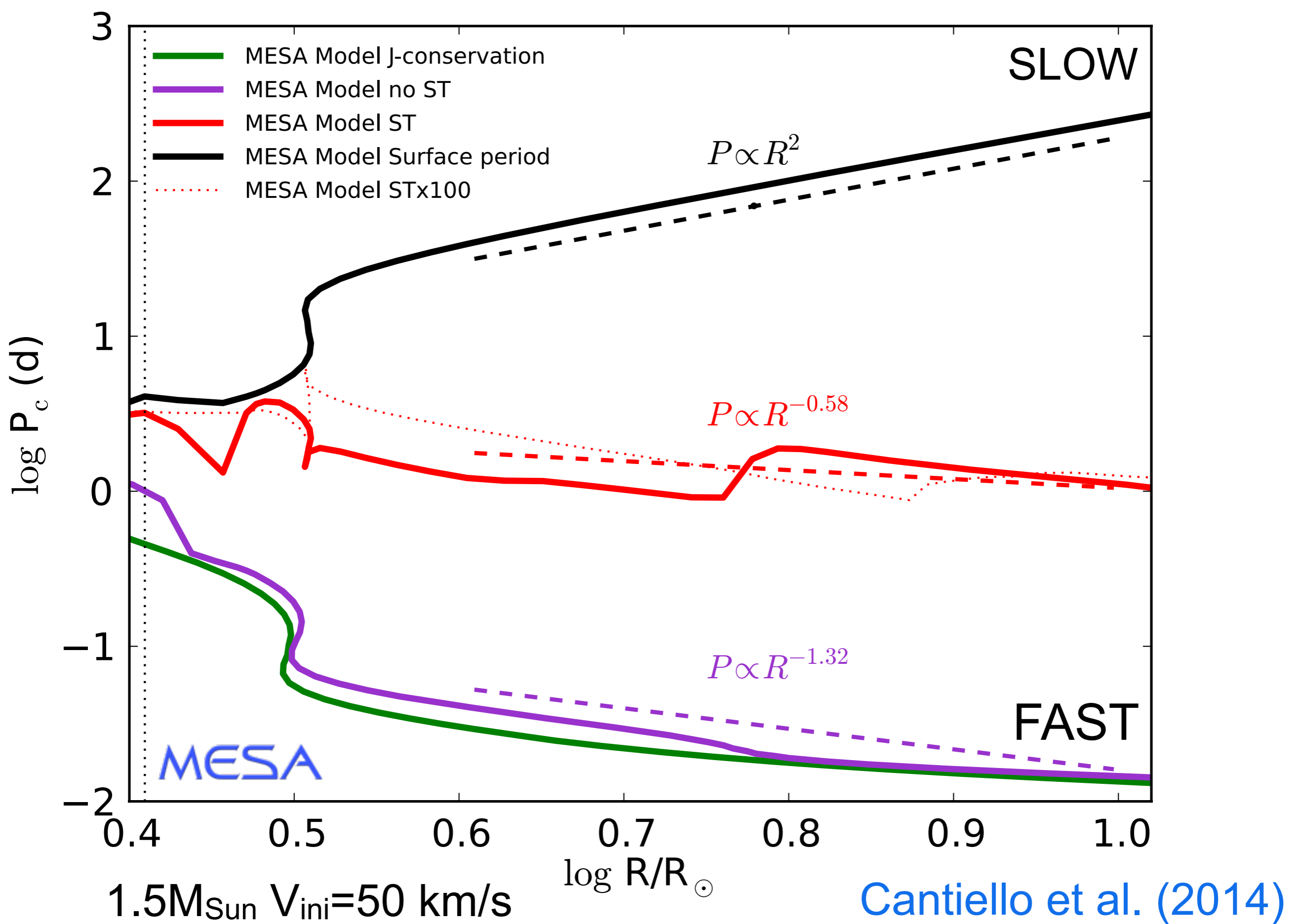
# **Red giants Asteroseismology**

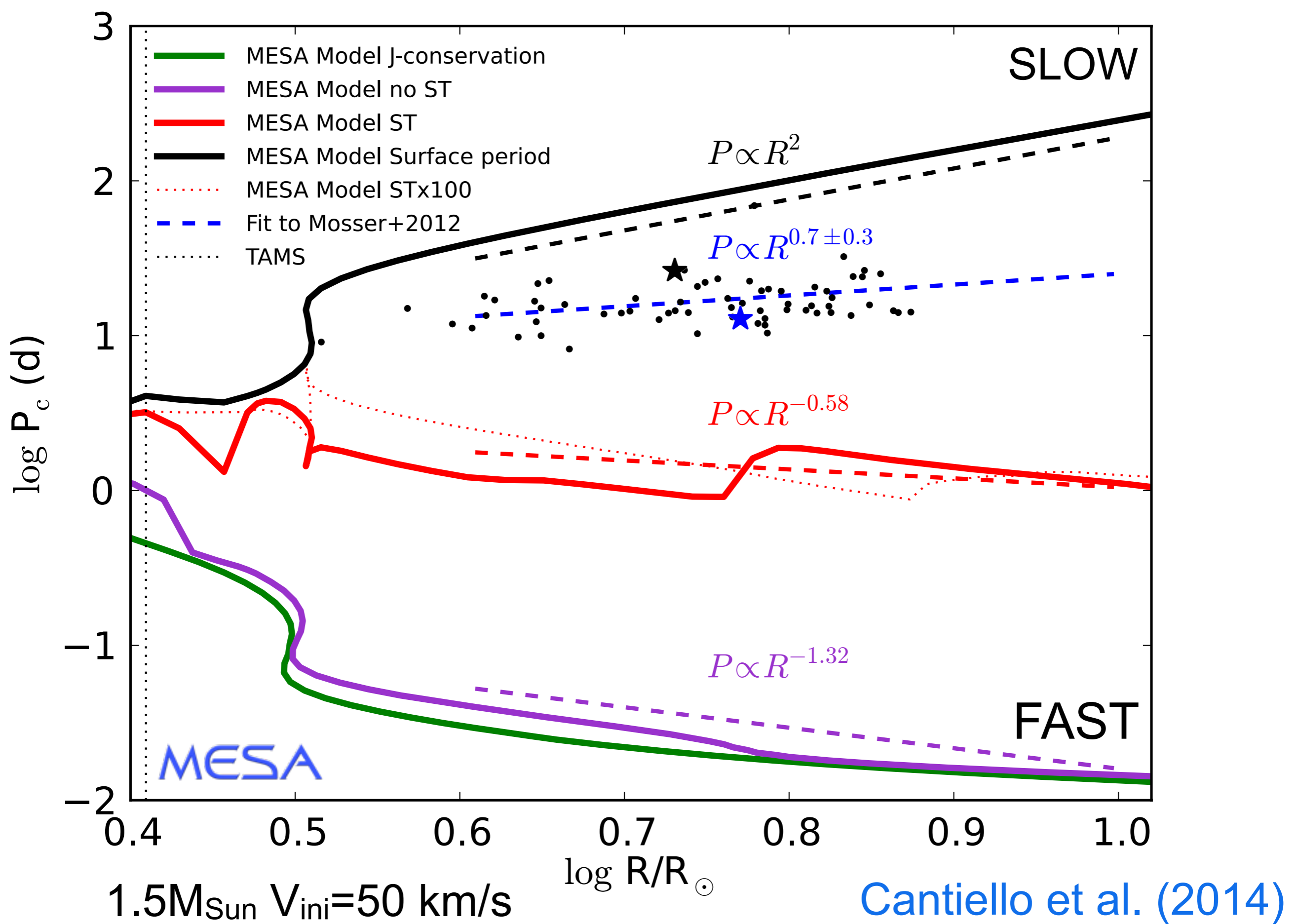
# Mixed Modes



Since a mixed mode lives both as a p-mode (in the envelope) and as a g-mode (in the core), if observed at the surface can give informations about conditions (e.g. **rotation rate**) in different regions of the star!

[Beck et al. 2012](#), [Mosser et al. 2012](#)

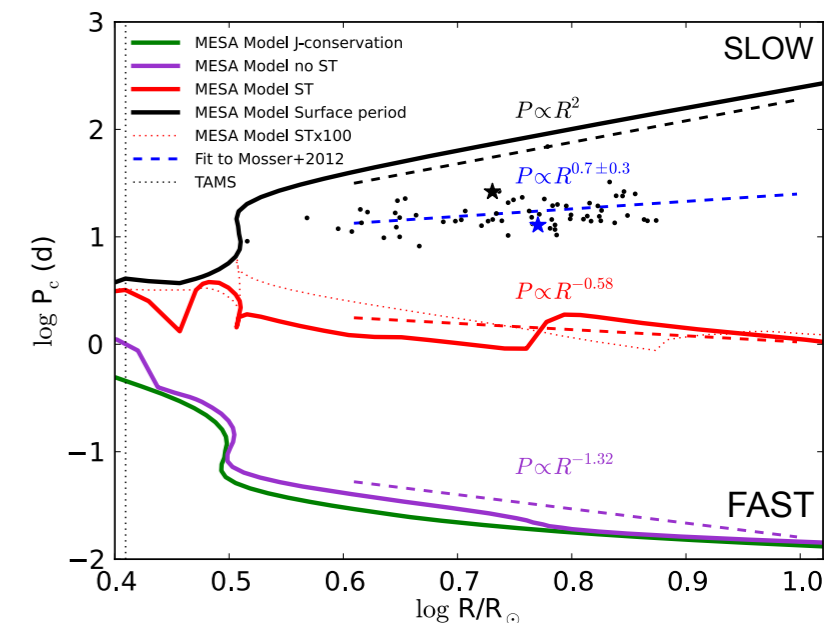
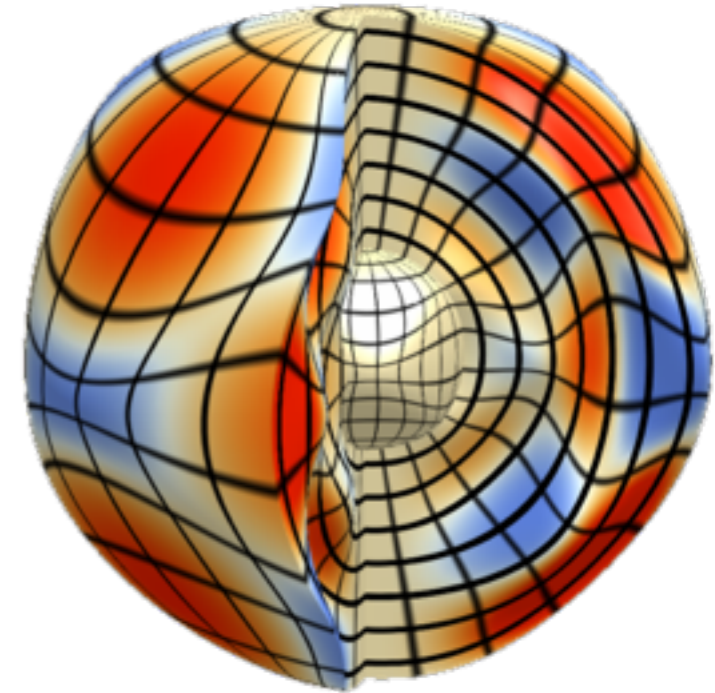




# Take Home Messages

- Thanks to space-based asteroseismology it is now possible to **access the internal rotational profile** of stars other than the Sun
- Despite great progress in last few years, the nature of **internal mixing of angular momentum** is still an **unsolved problem**

Credits: R. Townsend



Cantiello et al. 2014, Fuller et al. 2014



# Conclusions

- Rotation and binarity play an important role for the evolution and final fate of massive stars
- In most codes rotation and the induced transport of angular momentum and chemical species are included in a 1D, diffusion approximation
- A number of physical processes are modeled. Indirect tests include surface abundances and remnant rotation rates
- In low-mass stars asteroseismology provides a way to directly probe the rotational evolution of stellar cores
- We still do not fully understand internal angular momentum transport in stars. More to do!